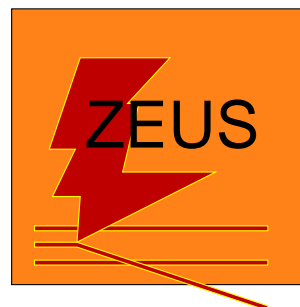


# What can Diffraction at HERA offer the LHC?

## Part 1: Diffractive pdf's and QCD factorization tests

Frank-Peter Schilling

[DESY]



### Contents:

- QCD factorization in diffraction
- Inclusive Diffractive DIS
- Determination of diffractive pdf's
- Factorization tests with jets and charm (HERA, Tevatron)



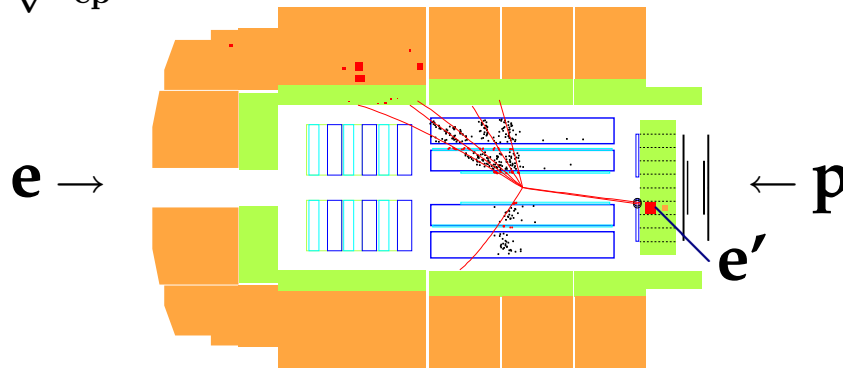
HERA-LHC Workshop  
Startup Meeting

CERN, March 26-27, 2004

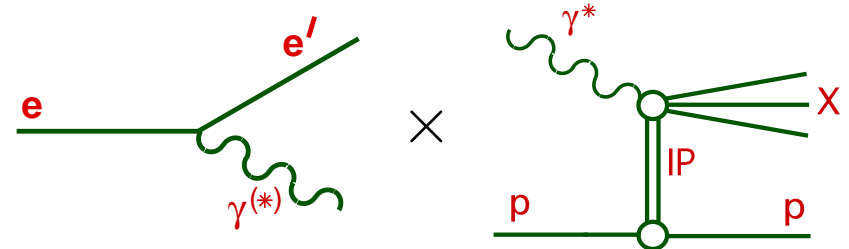
# Diffraction at HERA

- HERA: An ideal laboratory to study **hard diffraction**:
- 10% of low- $x$  DIS events are diffractive

$$\sqrt{s_{ep}} = 320 \text{ GeV}$$



Can be viewed as diffractive  $\gamma^* p$  interaction:



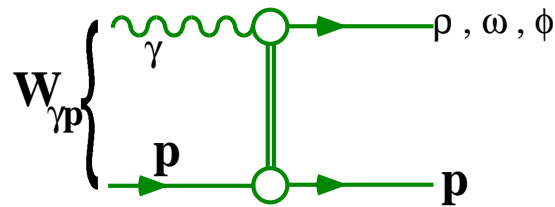
## Virtual photon $\gamma^*$ as a probe

- Inclusive DIS:  
Probe proton structure ( $F_2(x, Q^2)$ )
- Diffractive DIS:  
Probe structure of  
colour singlet exchange!

## Why diffraction?

- Diffraction is significant part of  $\sigma_{\text{tot}}$
- Novel tool to study **soft-hard transition in QCD**
- **Low- $x$  structure of the proton**  
(e.g. saturation)

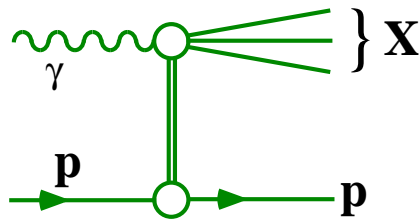
## Diffractive Processes in $\gamma p$ Interactions



QUASI ELASTIC  
VECTOR MESON  
PRODUCTION

(EL)

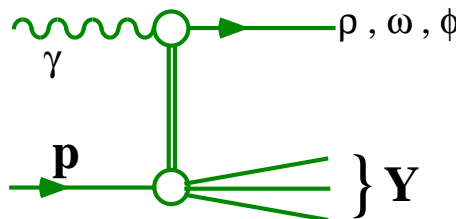
$$\gamma p \longrightarrow V p$$



SINGLE PHOTON  
DISSOCIATION

(GD)

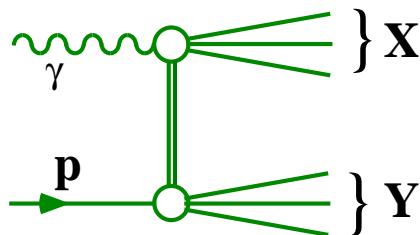
$$\gamma p \longrightarrow X p$$



SINGLE PROTON  
DISSOCIATION

(PD)

$$\gamma p \longrightarrow V Y$$



DOUBLE  
DISSOCIATION

(DD)

$$\gamma p \longrightarrow X Y$$

- All 4 processes can be measured with varying  $Q^2$ ,  $W$ ,  $t$ ,  $M_X$ ,  $M_Y$

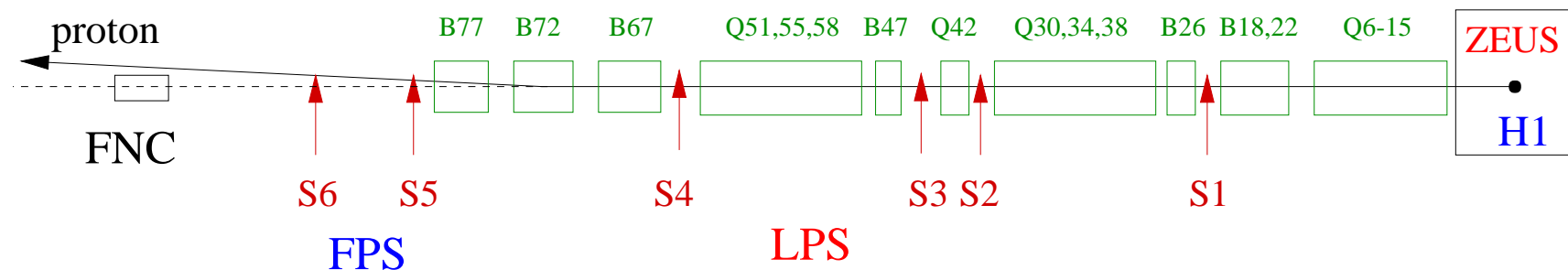
- large  $Q^2$ :  
 $\gamma^*$  probes diffractive exchange  
This talk!

- large  $|t|$ : perturbative QCD applicable to  $IP$  (BFKL)?

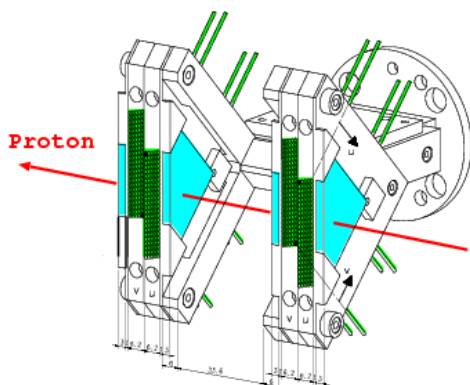
- $Q^2 \sim 0$ ,  $|t| \sim 0$ :  
similar to soft hadronic diffraction

Exclusive diffraction (VM, DVCS, ...):  
see Michele's talk!

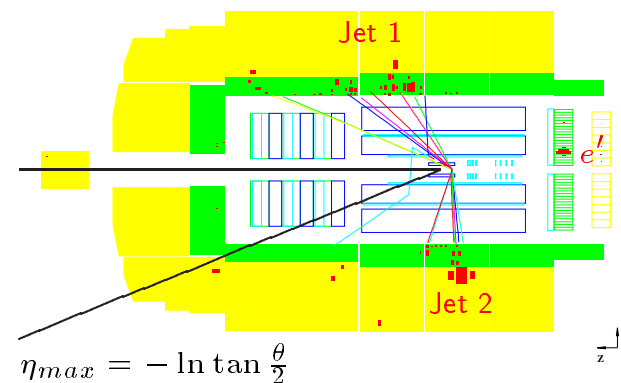
## Experimental Techniques



Forward Proton Spectrometers  
at  $z = 24 \dots 90$  m



Rapidity Gap Selection  
in central detector



### Measure leading proton

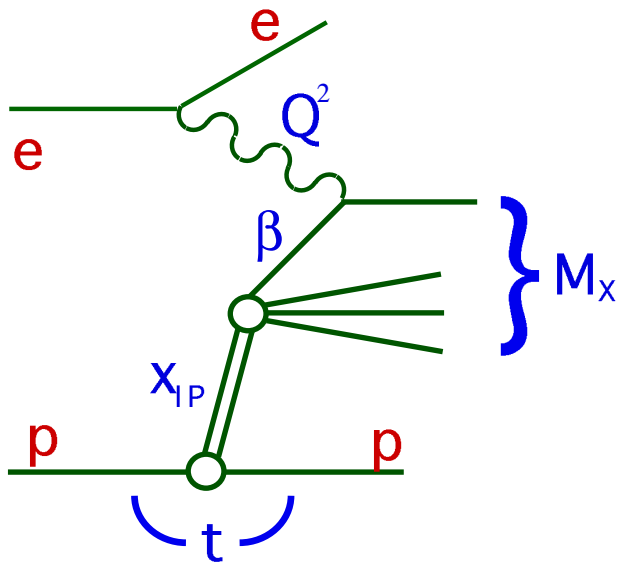
- Free of dissociation bkgd.
- Measure  $p$  4-momentum
- low statistics (acceptance)

### Require large rapidity gap

- $\Delta\eta$  large when  $M_{\text{central}} \ll W_{\gamma p}$
- integrate over outgoing  $p$  system
- high statistics (similar:  $M_X$  method)

## Diffractive Cross section and Structure Functions

In a frame where the proton is moving fast:



$$x_{IP} = \xi = \frac{Q^2 + M_X^2}{Q^2 + W^2} = x_{IP/p}$$

(momentum fraction of colour singlet exchange)

$$\beta = \frac{Q^2}{Q^2 + M_X^2} = x_{q/IP}$$

(fraction of exchange momentum of  $q$  coupling to  $\gamma^*$ ,  $x = x_{IP}\beta$ )

$$t = (p - p')^2$$

(4-momentum transfer squared)

Diffractive reduced cross section  $\sigma_r^D$ :

$$\frac{d^4\sigma}{dx_{IP} dt d\beta dQ^2} = \frac{4\pi\alpha^2}{\beta Q^4} \left(1 - y + \frac{y^2}{2}\right) \sigma_r^{D(4)}(x_{IP}, t, \beta, Q^2)$$

Structure functions  $F_2^D$  and  $F_L^D$ :

$$\sigma_r^{D(4)} = F_2^{D(4)} - \frac{y^2}{2(1-y+y^2/2)} F_L^{D(4)}$$

Integrated over  $t$ :  $F_2^{D(3)} = \int dt F_2^{D(4)}$

– Longitudinal  $F_L^D$ : affects  $\sigma_r^D$  at high  $y$

[ $\gamma$  inelasticity  $y = Q^2/sx$ ]

– If  $F_L^D = 0$ :  $\sigma_r^D = F_2^D$

## Factorization in Diffraction

### Diffractive pdf's / proof of QCD Factorization for diffractive DIS:

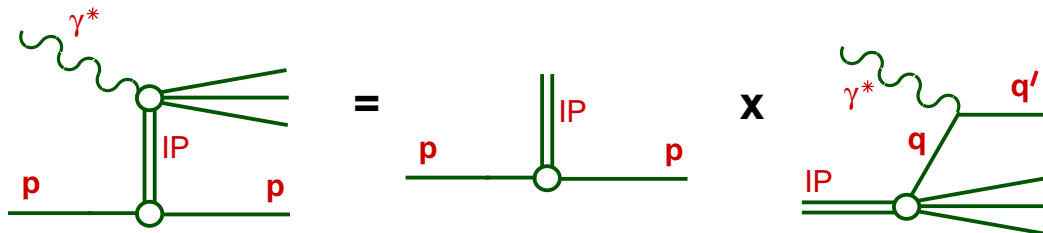
- Diffractive parton distributions (Trentadue, Veneziano, Berera, Soper, Collins, ...):

$$\frac{d^2\sigma(x, Q^2, x_{\mathbb{P}}, t)^{\gamma^* p \rightarrow p' X}}{dx_{\mathbb{P}} dt} = \sum_i \int_x^{x_{\mathbb{P}}} d\xi \hat{\sigma}^{\gamma^* i}(x, Q^2, \xi) p_i^D(\xi, Q^2, x_{\mathbb{P}}, t) \quad (+\text{higher twist})$$

- $\hat{\sigma}^{\gamma^* i}$  hard scattering coeff. functions, as in incl. DIS
- $p_i^D$  diffractive PDF's in proton, conditional probabilities, valid at fixed  $x_{\mathbb{P}}, t$ , obey (NLO) DGLAP

### Ingelman-Schlein Model ('Resolved Pomeron' model):

$x_{\mathbb{P}}, t$  dependence factorizes out (Donnachie, Landshoff, Ingelman, Schlein, ...):

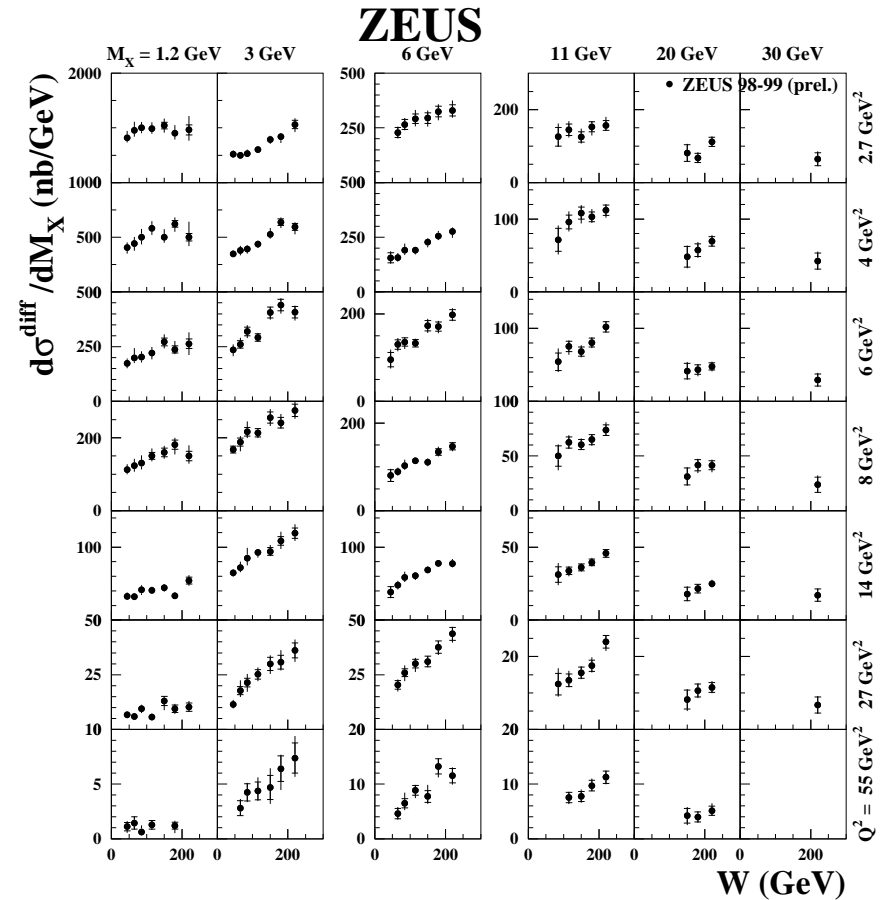
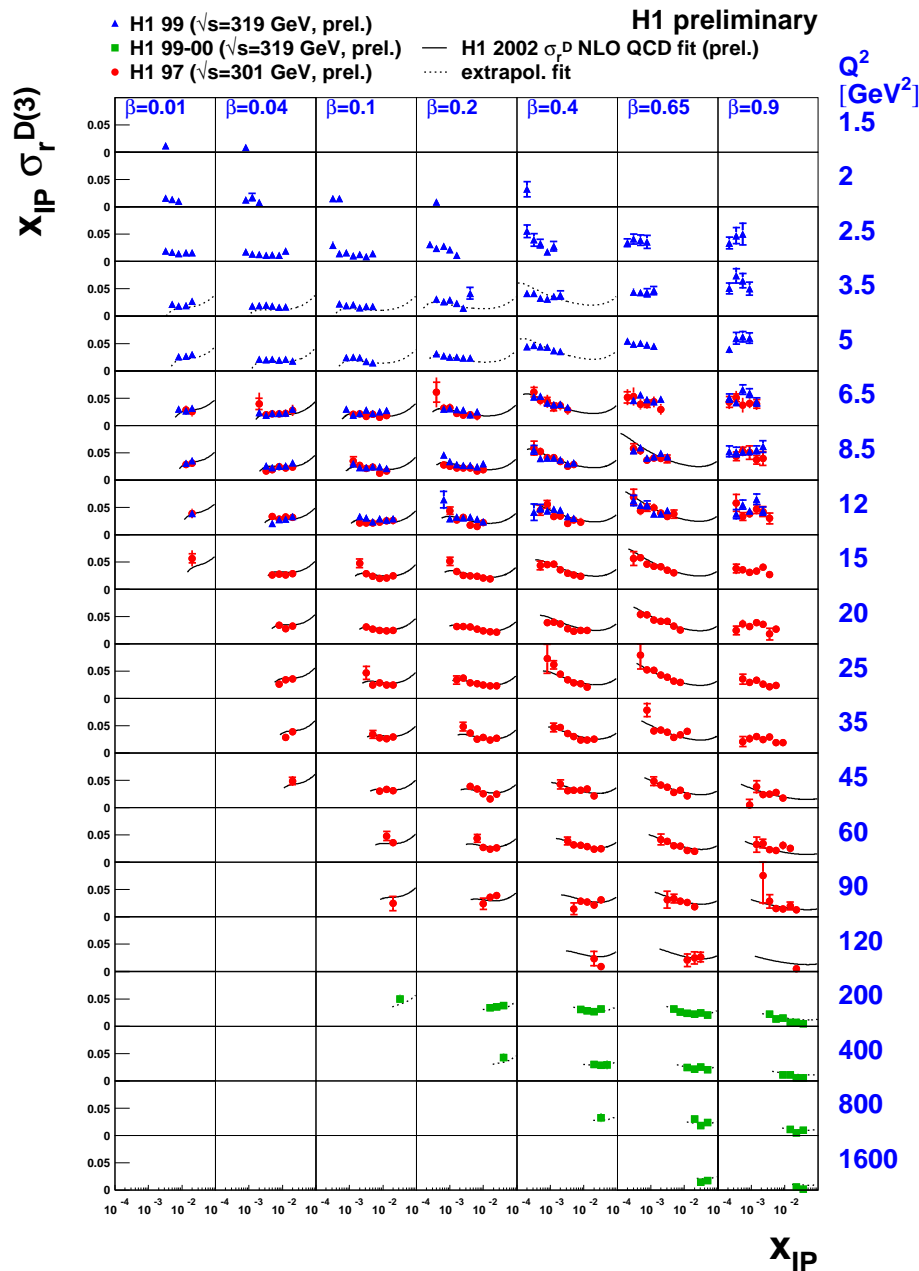


- additional assumption, **no proof!**
- consistent with present data if sub-leading  $\mathbb{R}$  included

$$F_2^D(x_{\mathbb{P}}, t, \beta, Q^2) = f_{\mathbb{P}/p}(x_{\mathbb{P}}, t) F_2^{\mathbb{P}}(\beta, Q^2)$$

Shape of diffr. PDF's indep. of  $x_{\mathbb{P}}, t$ , normalization controlled by Regge flux  $f_{\mathbb{P}/p}$

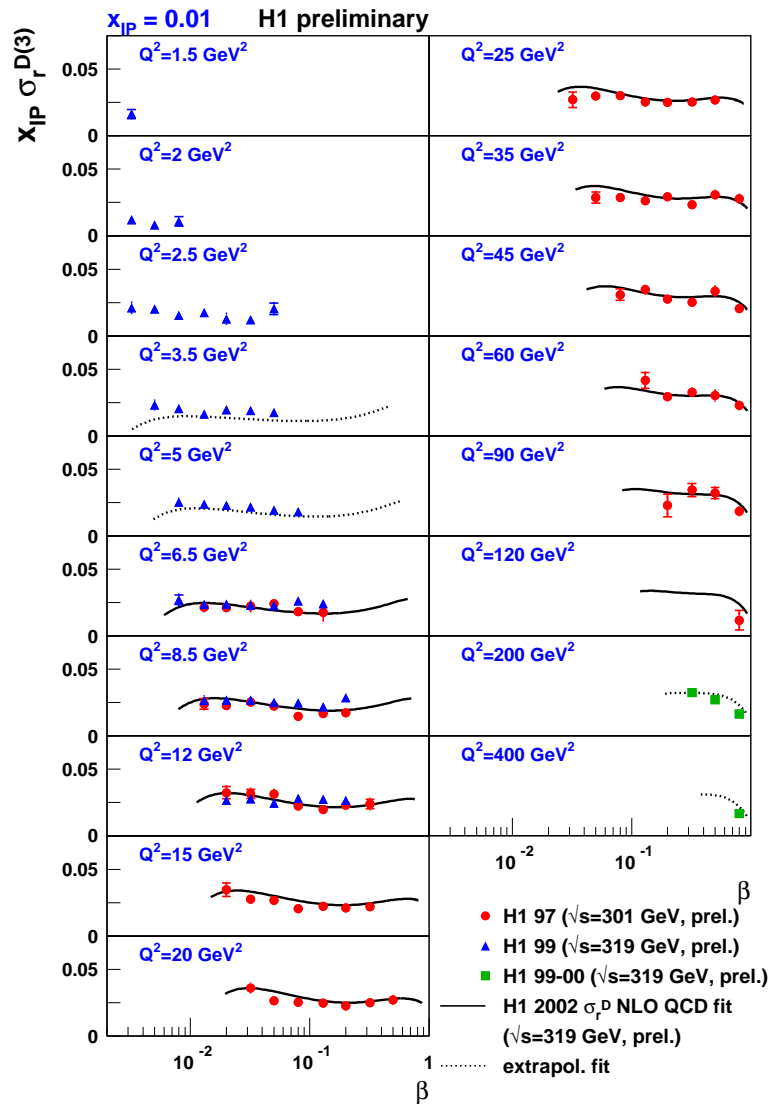
# Recent Diffractive DIS cross section data



- Large kinematic range covered
- $1.5 < Q^2 < 1600$  GeV<sup>2</sup>
- large stat. precision
- At low  $Q^2$  limited by syst. err. from diffractive selection

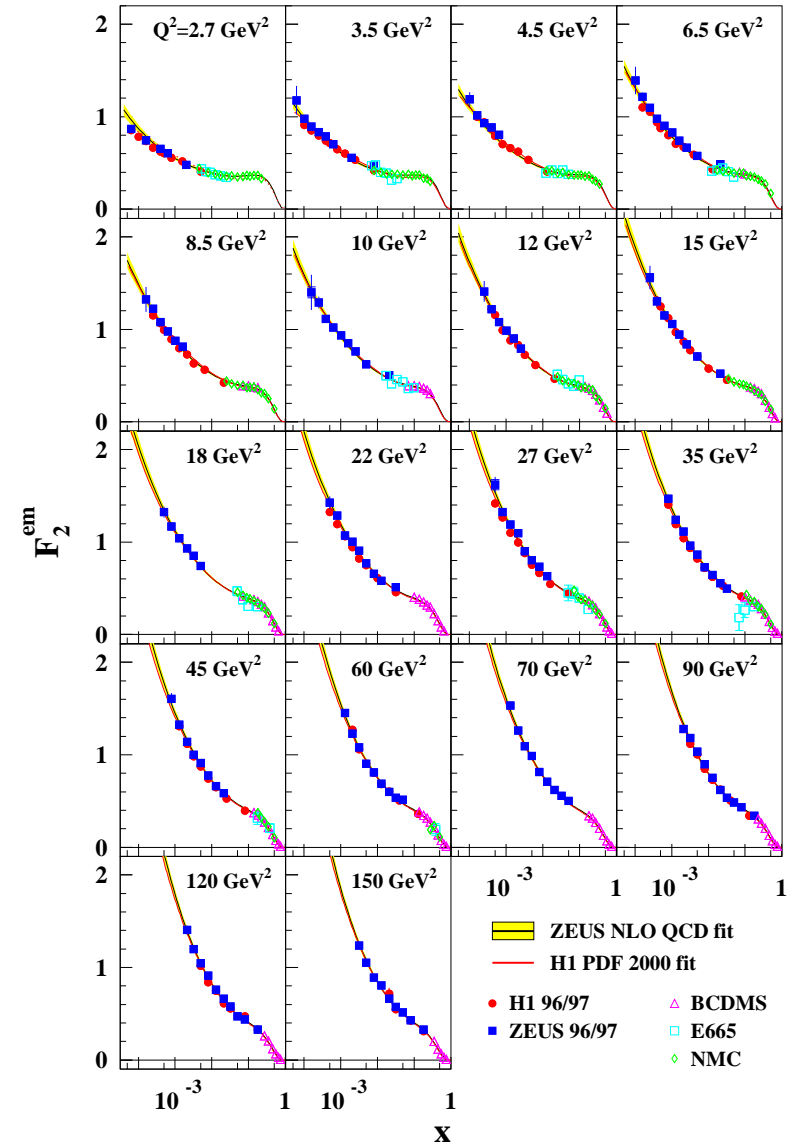
# Comparison diffractive vs inclusive: $\beta$ or $x$ dependence

## Diffractive:



## Proton:

### HERA $F_2$

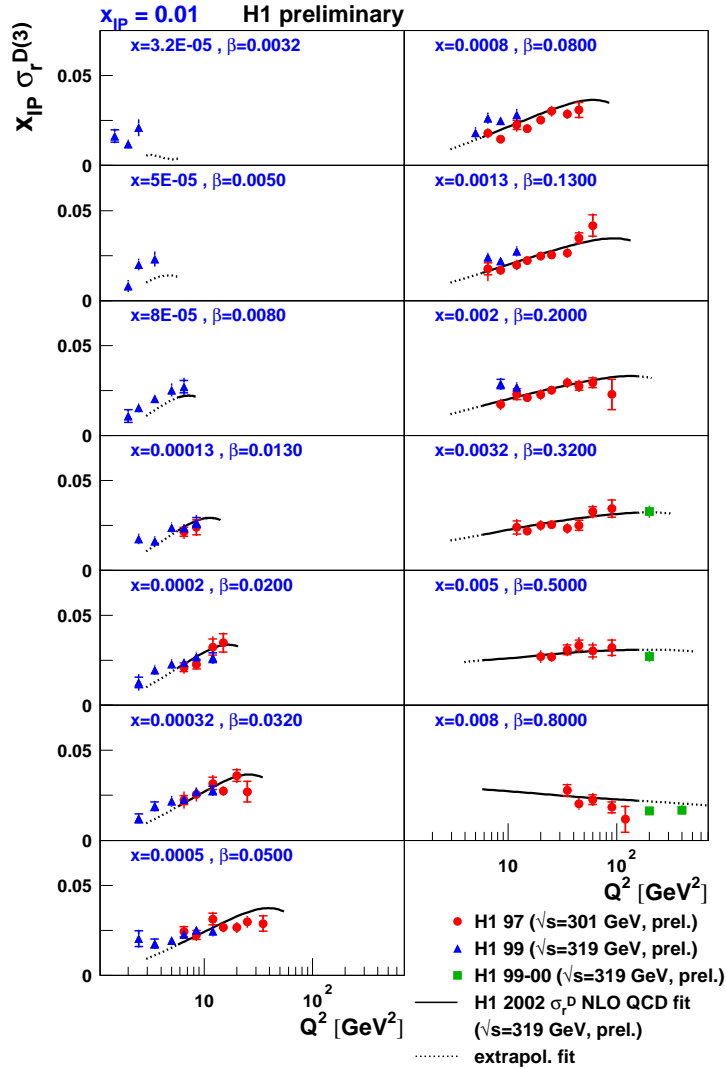


⇒ Only weak  $\beta$  dependence! Similar to photon ...

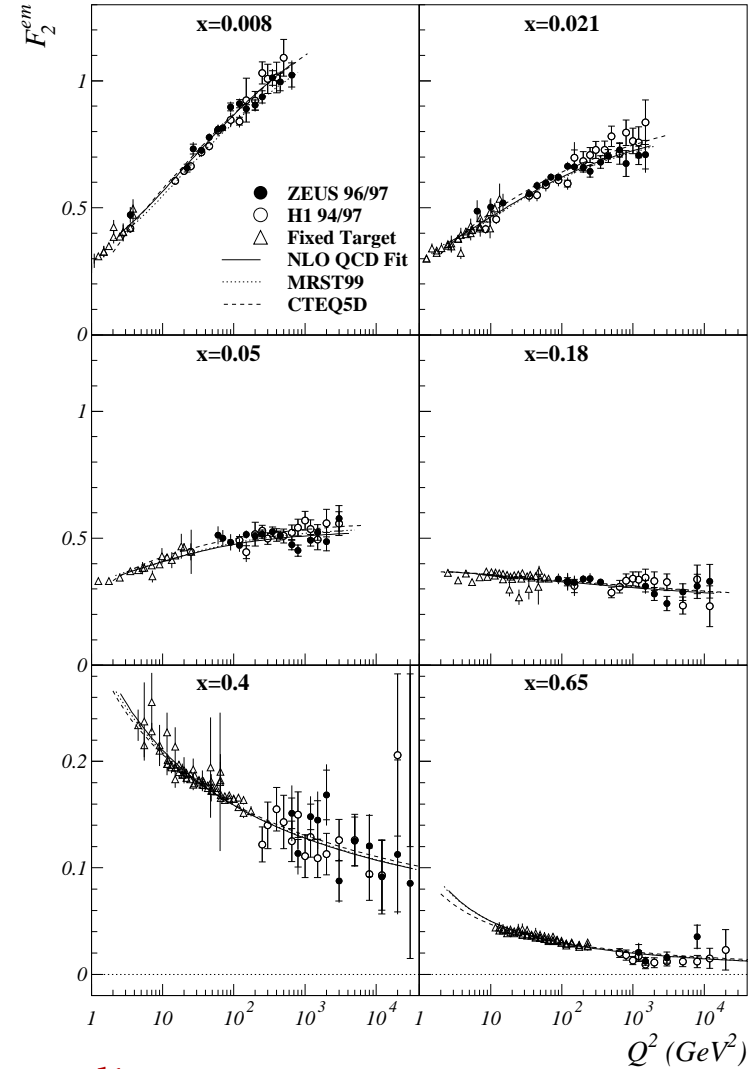


# Comparison diffractive vs inclusive: $Q^2$ dependence

## Diffractive:



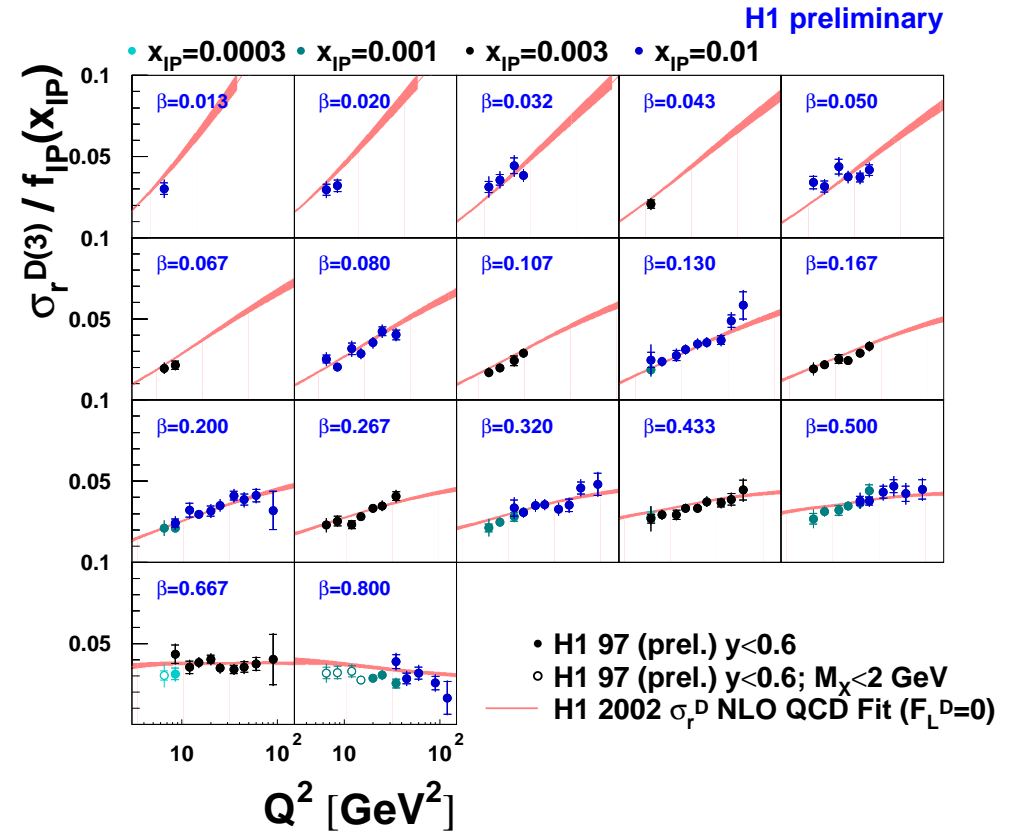
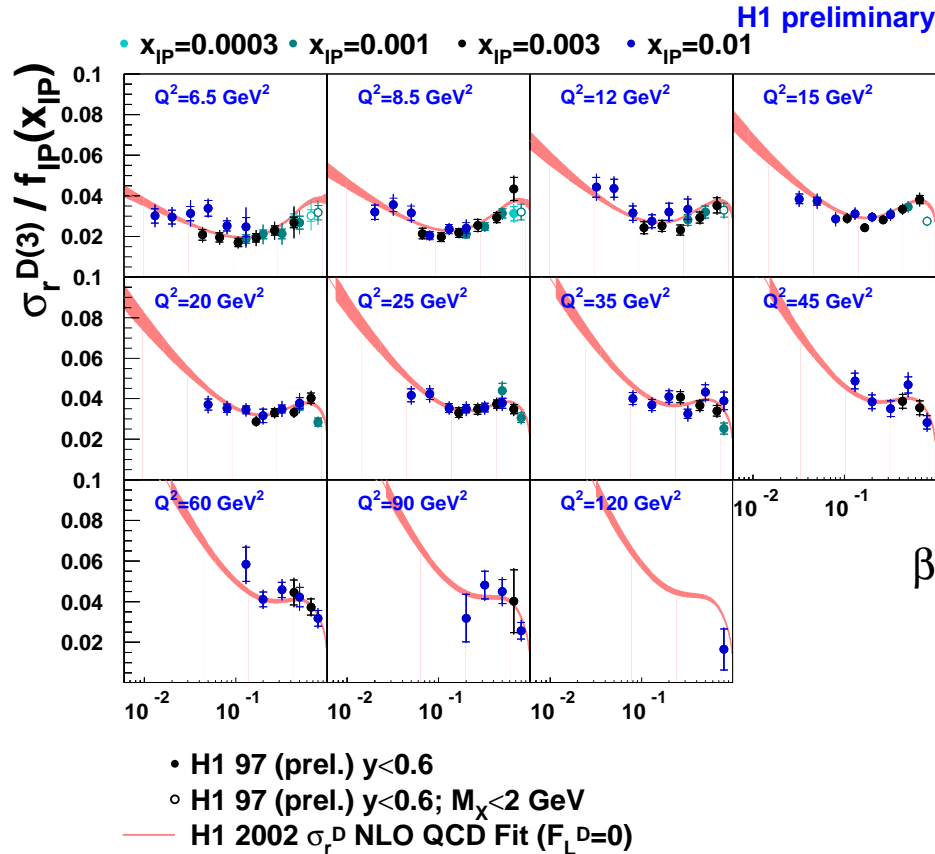
## Proton: ZEUS



⇒ +ve scaling violations to highest  $\beta$ : Gluon dominated!

# Precise H1 Measurement of $\beta, Q^2$ dependences

Prerequisite for NLO DGLAP QCD fit:



$$\beta \text{ dep.} \cdot \sim \sum_i e_i^2 (q_i^D + \bar{q}_i^D)$$

$$d\sigma/d \ln Q^2 \cdot \sim \alpha_s \otimes g^D(\beta, Q^2)$$

- $x_{IP}$  dep. taken out: factorization holds for  $x_{IP} < 0.01$
- rising for  $\beta \rightarrow 1$  at low  $Q^2$
- positive scaling violations expect for largest  $\beta$  (gluon dominance)

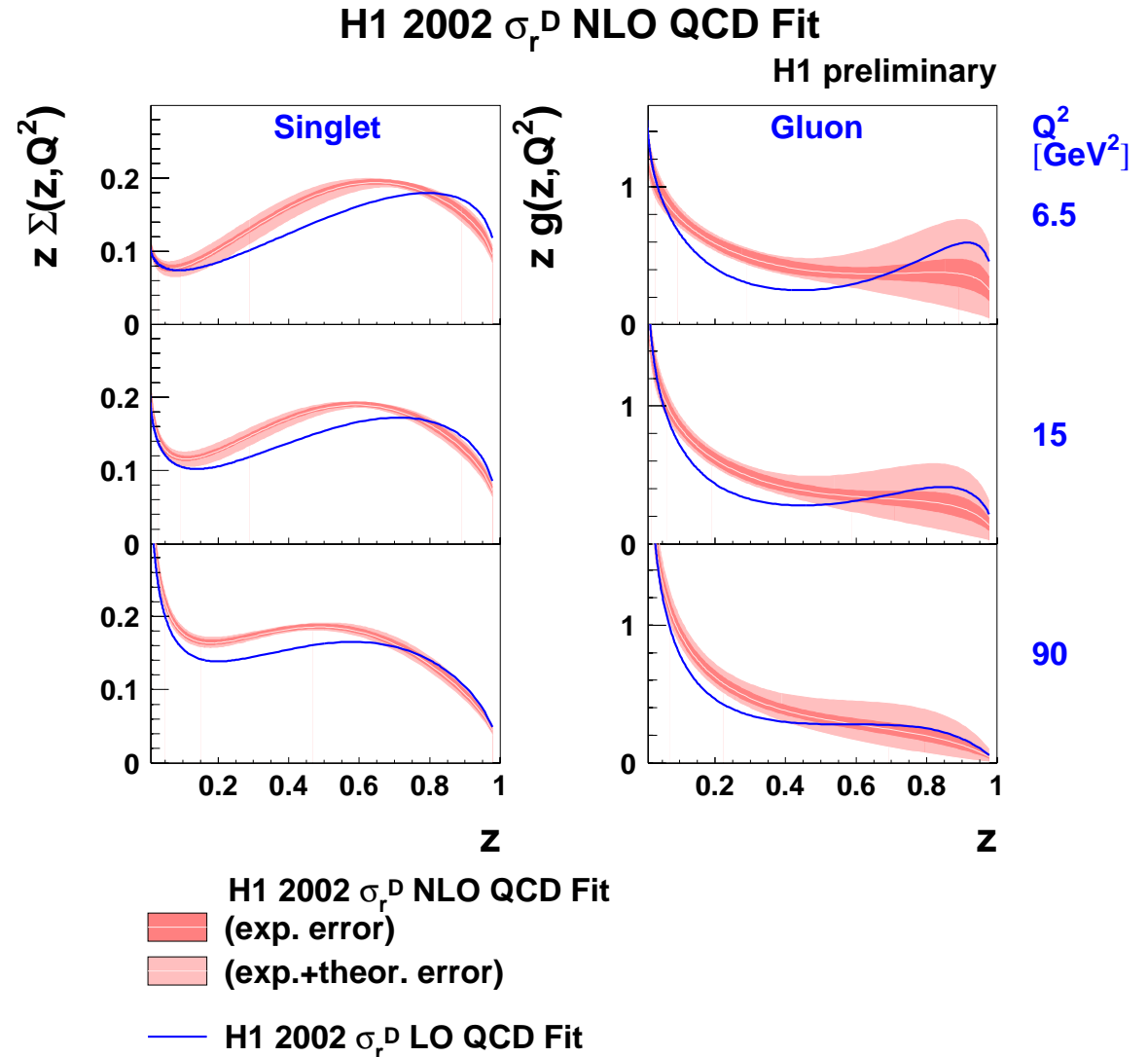
## NLO DGLAP QCD Fit (H1)

### QCD Fit Technique:

- factorize  $f(x_{\mathbb{P}})f(z, Q^2)$
- Singlet  $\Sigma$  and gluon  $g$  parameterized at  $Q_0^2 = 3 \text{ GeV}^2$
- NLO DGLAP evolution
- Fit data for  $Q^2 > 6.5 \text{ GeV}^2, M_X > 2 \text{ GeV}$
- **For first time propagate exp. and theor. uncertainties !**

### PDF's of diffractive exchange:

- Extending to large fractional momenta  $z$
- **Gluon dominated**
- $\Sigma$  well constrained
- substantial uncertainty for gluon at highest  $z$
- Similar to previous fits



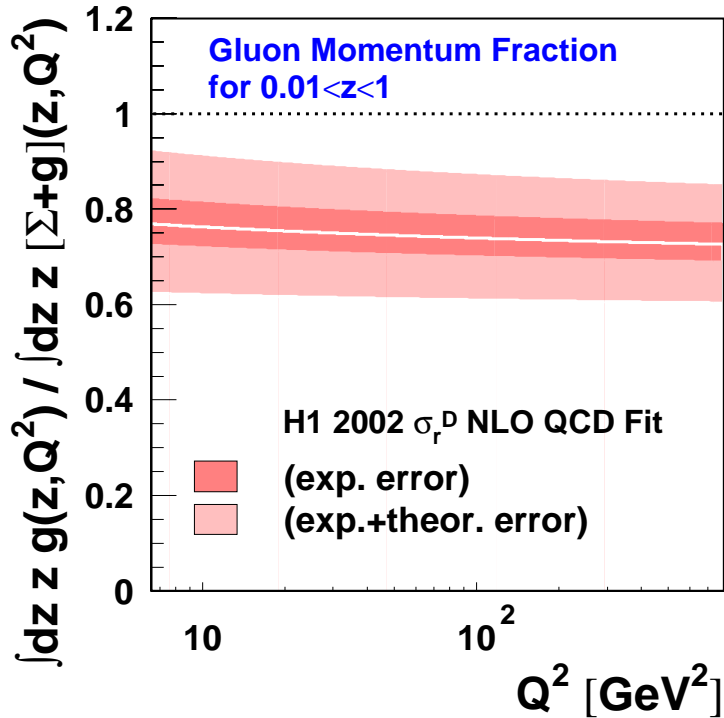
# H1 NLO QCD Fit: Gluon fraction and $F_L^D$

Integrate PDF's over measured range:

Longitudinal  $F_L^D$ :

$$F_L^D \sim \frac{\alpha_s}{2\pi} \left[ C_q^L \otimes F_2^D + C_g^L \otimes \sum_i e_i^2 z g^D(z, Q^2) \right]$$

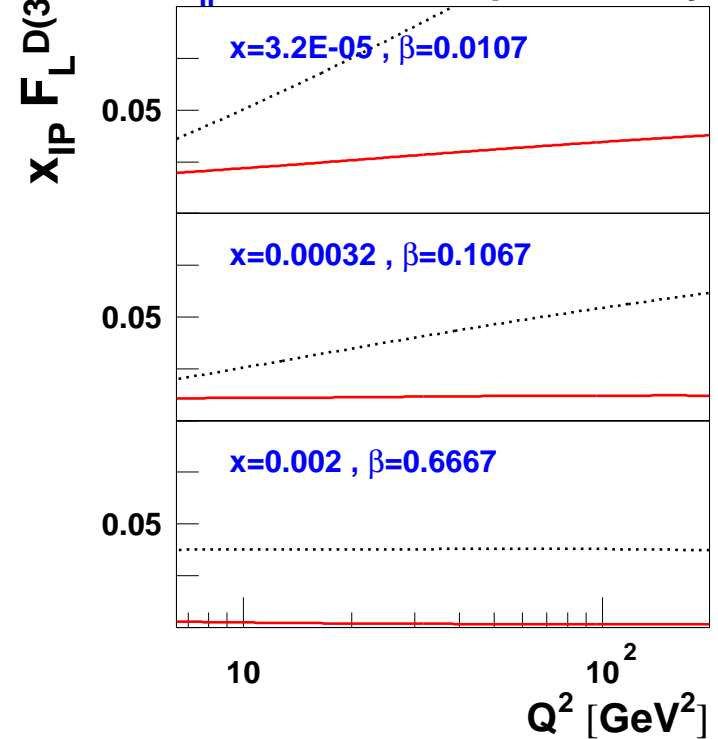
H1 preliminary



Momentum fraction of diffractive exchange carried by gluons:

$$75 \pm 15\%$$

$x_{IP} = 0.003$  H1 preliminary

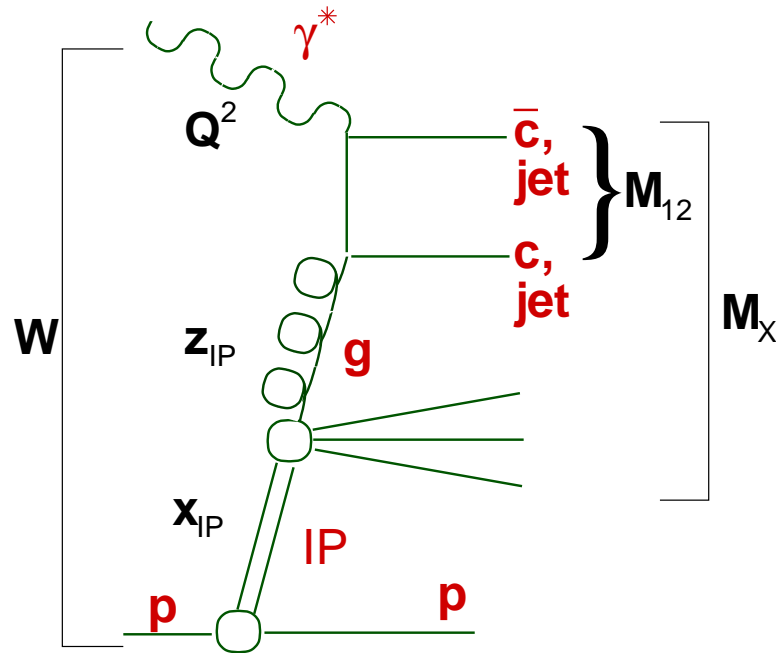


—  $F_L^D$  (from NLO QCD Fit)  
 .....  $F_2^D$

$\Rightarrow F_L^D$  large at low  $Q^2$ , low  $\beta$

## Jet and Open Charm Production in Diffractive DIS

Test QCD factorization by applying dpdf's to final state cross sections ...



$Q^2$ : Photon virtuality

$W$ :  $\gamma^* p$  CMS energy

$M_X$ : mass of diffractively produced system

$M_{12} = \sqrt{\hat{s}}$ : mass of two jets /  $c\bar{c}$  pair

$$x_{IP} = \frac{Q^2 + M_X^2}{Q^2 + W^2}$$

momentum fraction of diffractive exchange w.r.t. proton

$$z_{IP} = \frac{Q^2 + M_{12}^2}{Q^2 + M_X^2}$$

momentum fraction of diffractive exchange entering hard process

→ High sensitivity to diffractive gluon distribution!

- high  $p_T$  jet production
- $c \rightarrow D^*$  Meson production

## NLO Calculations for Diffractive Final States

- So far mostly LO Monte Carlo programs with parton showers used
- QCD factorization: Hard scattering cross section same as for normal DIS
- NLO important to describe non-diffractive Jet production

→ use standard NLO programs for jets and heavy quarks in DIS ( $\mathcal{O}(\alpha_s^2)$ )

### Diffractive DIS Jets:

Use DISENT (Seymour)  
c.f. Hautmann [JHEP 0210 (2002) 025]

Calculate NLO cross section at fixed  $x_{\mathbb{P}}$  by  
running with reduced  $E_p = x_{\mathbb{P}} E_{p,nom.}$

Use diffractive pdf  $p_{i/\mathbb{P}}(z, \mu^2)$

Mul. w/ flux  $f_{\mathbb{P}}(x_{\mathbb{P}}) = \int dt f_{\mathbb{P}}(x_{\mathbb{P}}, t)$

Data integrated over  $x_{\mathbb{P}}$ :

“ $x_{\mathbb{P}}$  slicing”

### Diffractive DIS $D^*$ :

Diffractive version of HVQDIS (Harris, Smith) by Alvero, Collins, Whitmore  
[hep-ph/9806340]

$x_{\mathbb{P}}, t$  integration numerically

NLO Calculation in massive scheme

Peterson fragmentation

Both Interfaced to H1 diffractive pdf's

## NLO Comparisons with Diffractive DIS Jets

### Data:

Published H1 data:

[Eur. Phys. J. **C20** (2001) 29]

$$4 < Q^2 < 80 \text{ GeV}^2, 0.1 < y < 0.7,$$

$$x_{\mathbb{P}} < 0.05$$

Jets: CDF cone,  $p_{T,jet} > 4 \text{ GeV}$

But: NLO unstable if  $p_{T,1} \sim p_{T,2}$

→ Data corrected to  $p_{T,1(2)} > 5(4) \text{ GeV}$

### NLO Calculations with DISENT:

$$\mu_r^2 = p_T^2, \mu_f^2 = 40 \text{ GeV}^2$$

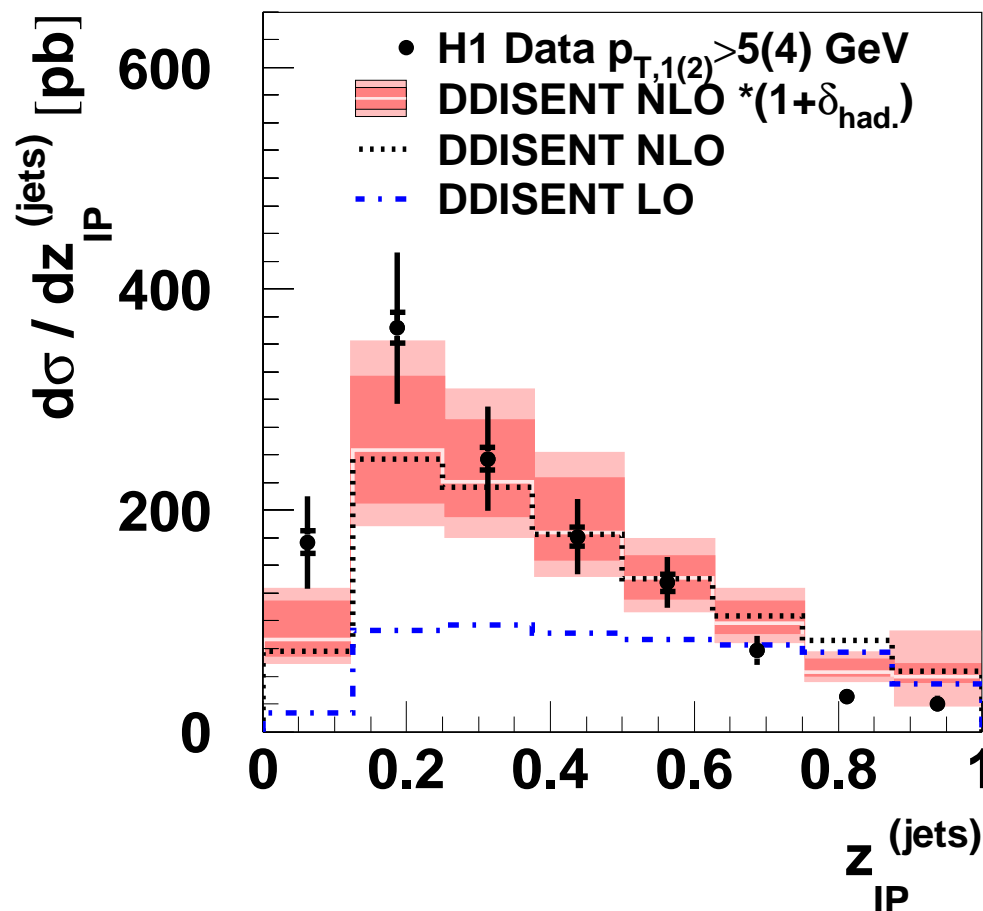
$$\Lambda_{QCD}^4 = 0.2 \text{ GeV}^4 \text{ (as in QCD fit)}$$

Hadronization corrections applied

Inner band:  $0.25\mu_r^2 \dots 4\mu_r^2$

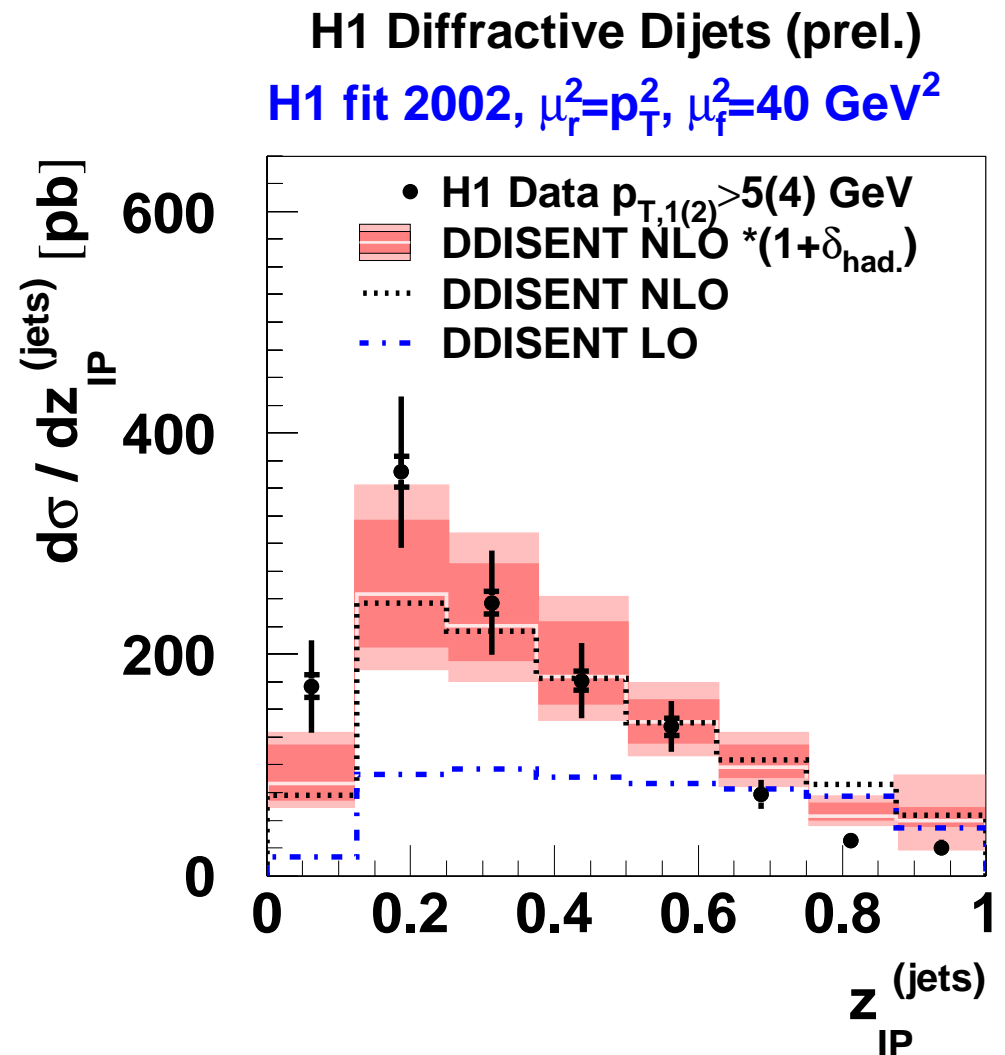
Outer band includes unc. in hadr. corr.

H1 Diffractive Dijets (prel.)  
H1 fit 2002,  $\mu_r^2 = p_T^2, \mu_f^2 = 40 \text{ GeV}^2$



## NLO Comparisons with Diffractive DIS Jets (cont.)

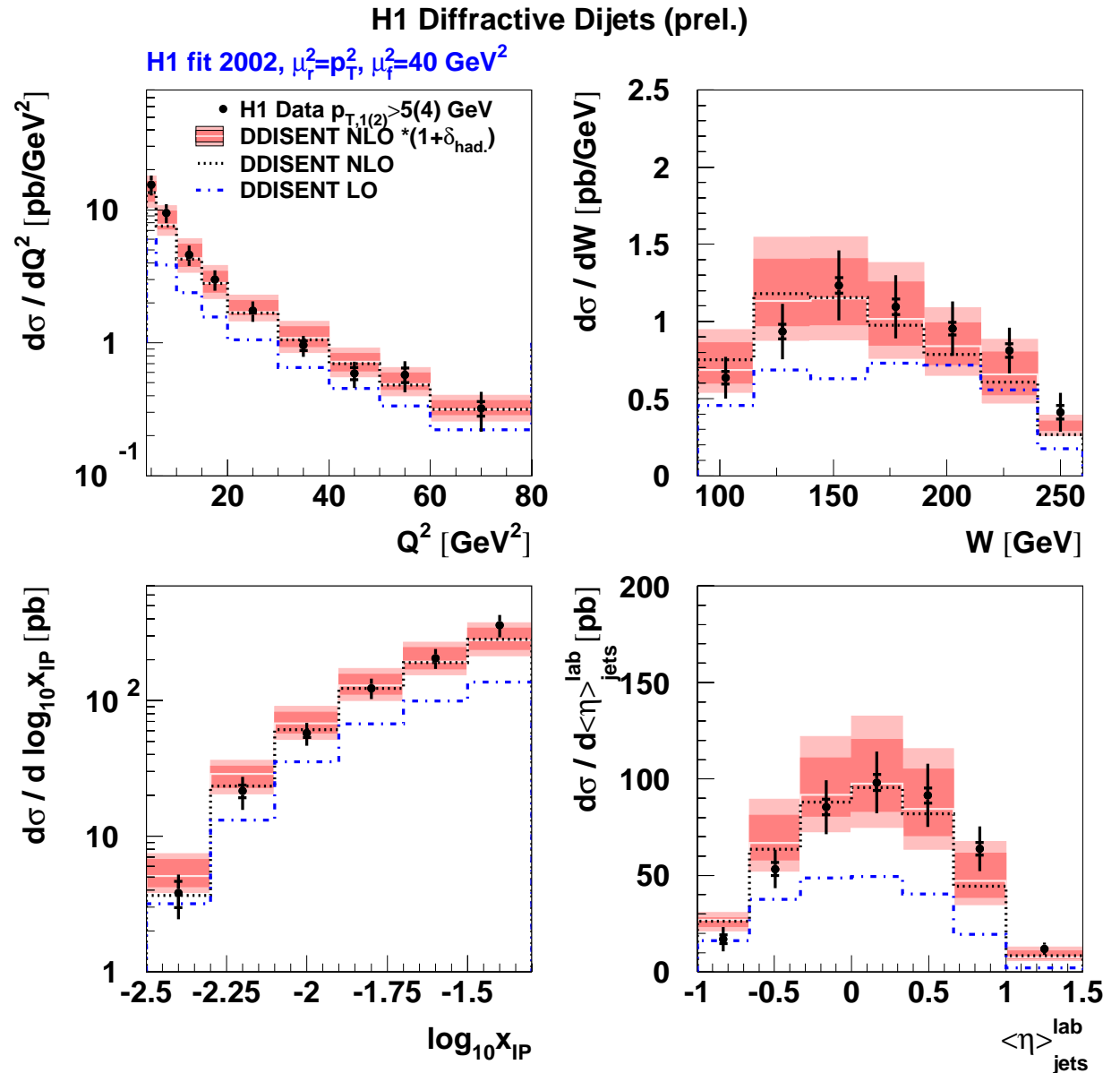
- Cross section differential in  $z_{IP}$
- LO Calculation too low, shape of data not reproduced (note: w/o parton showers!)
- Size of NLO correction on average factor  $\sim 2$  (due to low jet  $p_T$ )
- NLO, corrected for hadronization: reasonable description in shape and normalization
- Renormalization scale unc.  $\sim 20\%$
- Not shown: pdf uncertainty (gluon at high  $z_{IP}$ )





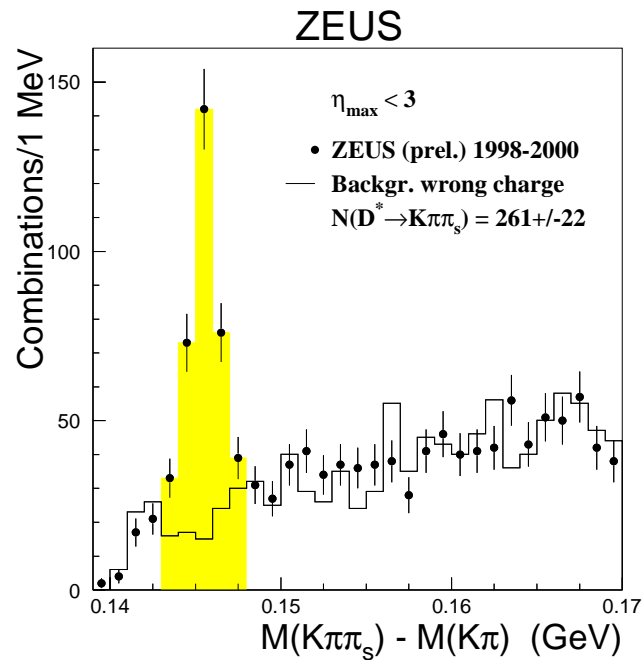
## NLO Comparisons with Diffractive DIS Jets (cont.)

- Further Cross sections:
- Size of NLO Corrections decreasing with  $Q^2$  (and  $p_T$ , not shown)
- Reasonable agreement with NLO calculation



## Diffractive Open Charm in DIS

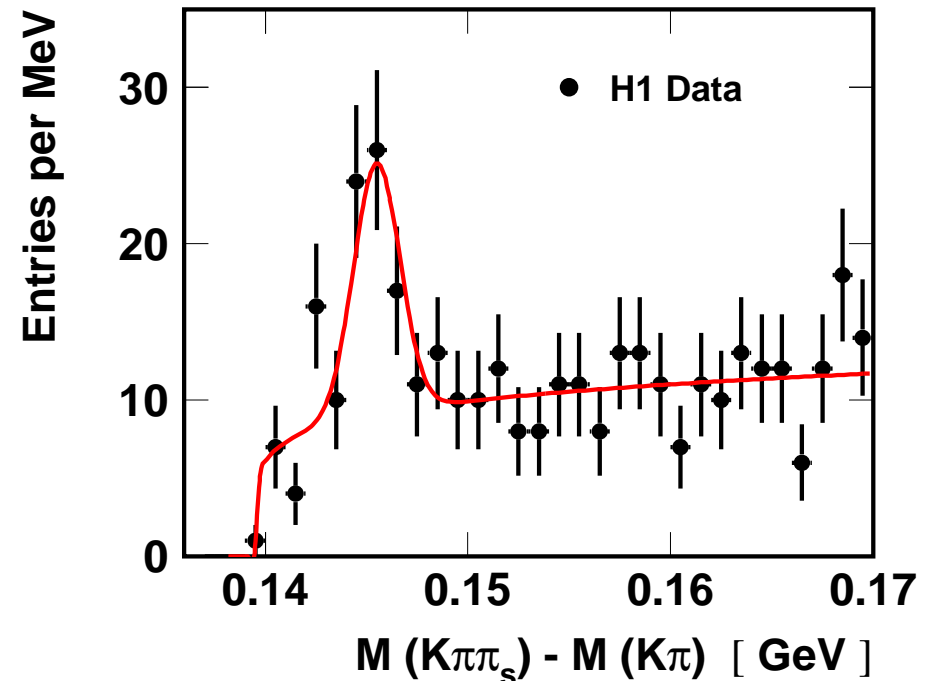
Use  $D^* \rightarrow D_0 \pi_s \rightarrow K \pi \pi_s$



$$1.5 < Q^2 < 200 \text{ GeV}^2$$

$$x_P < 0.035$$

$$p_{T,D^*} > 1.5 \text{ GeV}, |\eta_{D^*}| < 1.5$$



$$2 < Q^2 < 100 \text{ GeV}^2$$

$$x_P < 0.04$$

$$p_{T,D^*}^* > 2 \text{ GeV}, |\eta_{D^*}| < 1.5$$

So far measurements statistics limited

# NLO Comparisons with Diffractive DIS $D^*$ (H1)

## NLO Calculations with diffr. HVQDIS:

$$\mu_r^2 = \mu_f^2 = Q^2 + 4m_c^2$$

$$\Lambda_{QCD}^4 = 0.2 \text{ GeV} \text{ (as in QCD fit)}$$

Peterson Fragmentation:  $\epsilon = 0.078$

$$m_c = 1.5 \text{ GeV}, f(c \rightarrow D^*) = 0.233$$

Inner NLO error band:  $0.25\mu_r^2 \dots 4\mu_r^2$

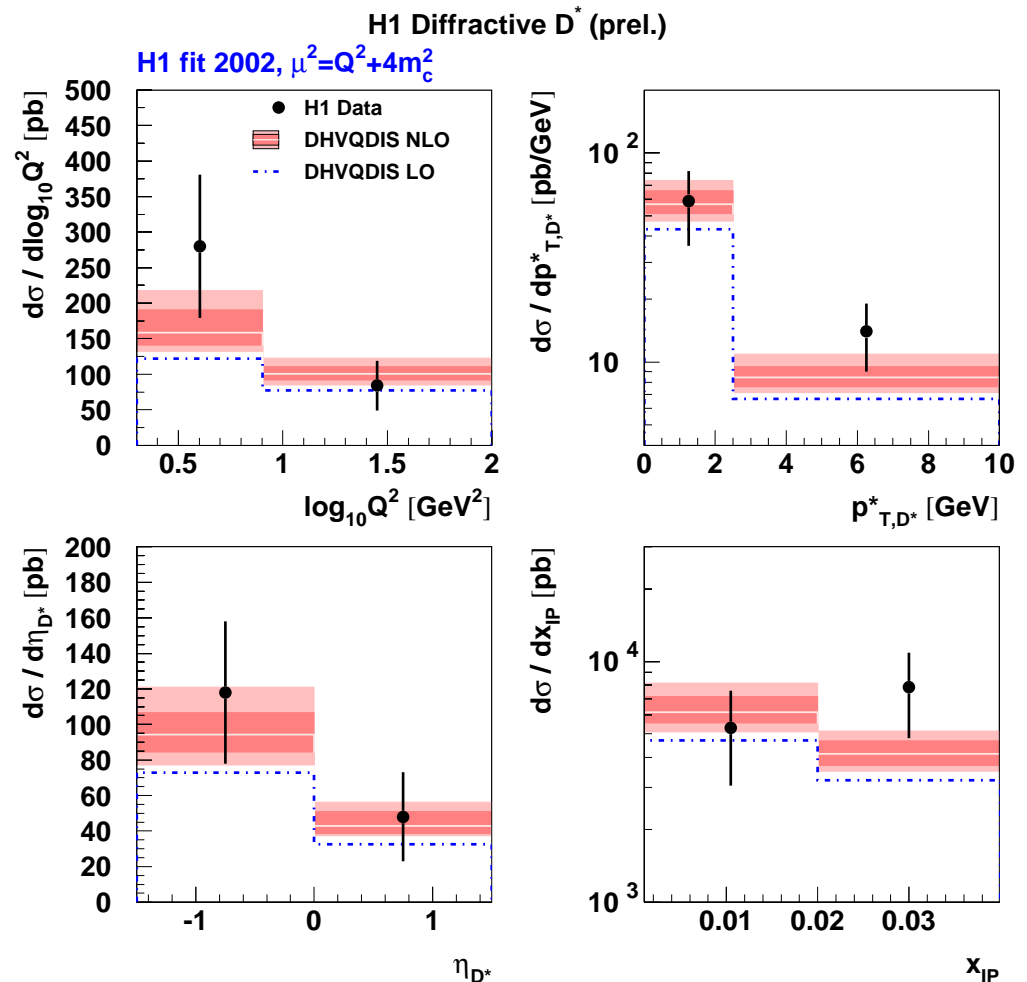
Outer band also includes

$$-1.35 < m_c < 1.65 \text{ GeV} (\pm 12\%)$$

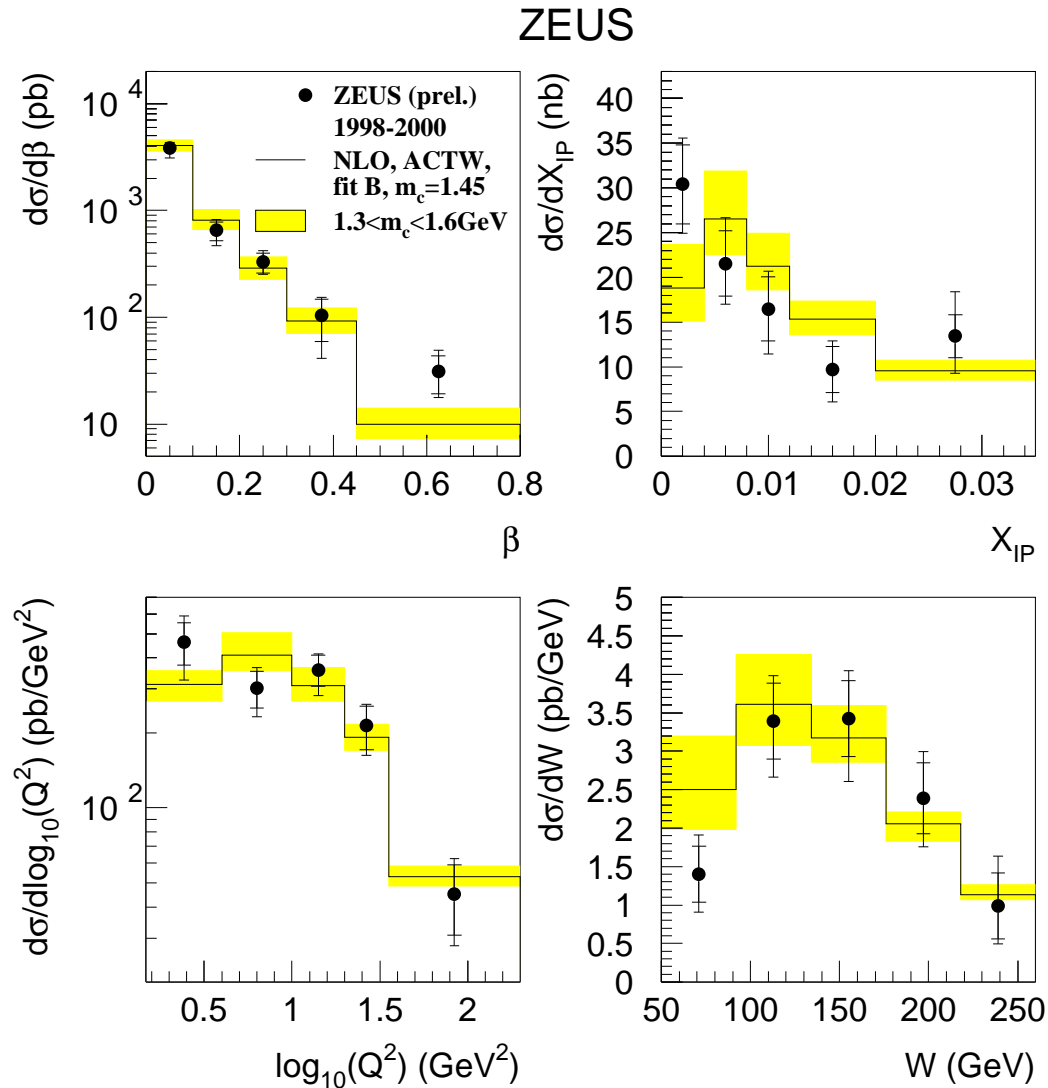
$$-0.035 < \epsilon < 0.100 (+21/ - 7\%)$$

Good agreement in shape and normalization within uncertainties

Size of NLO correction smaller than for dijets



## Diffractive $D^*$ in DIS (ZEUS)

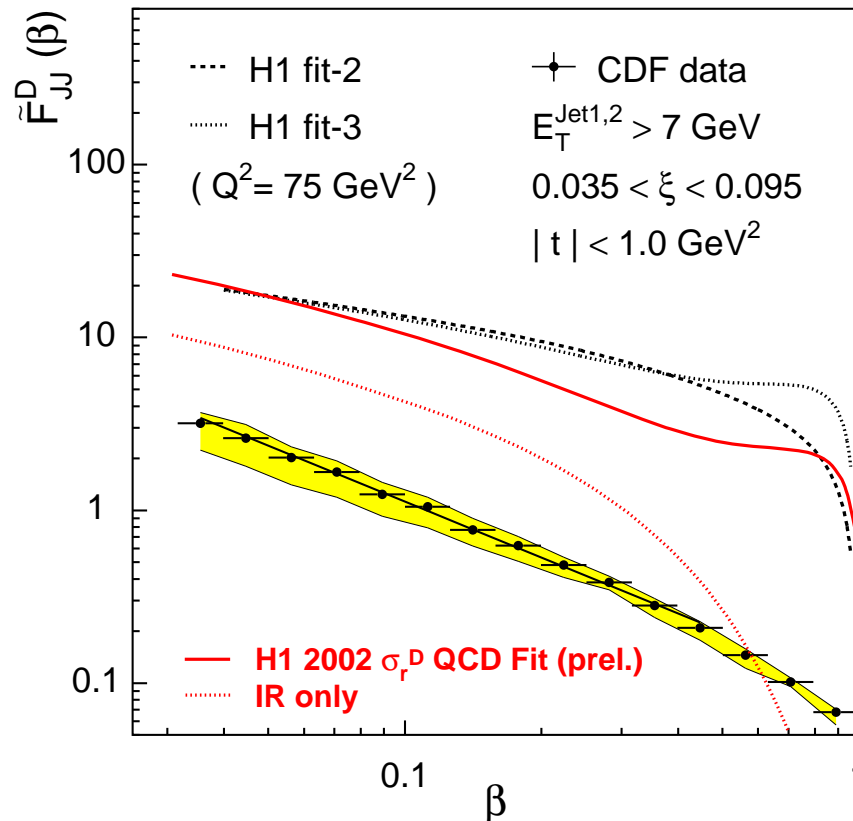


- Theory: gluon dominated pdf's from inclusive fits (ACTW), interfaced to NLO matrix elements
- Differential cross sections well described by calculation!

⇒ Support for QCD factorization in diffractive DIS!

## Diffractive Dijets at the Tevatron (CDF)

Use pdf's to predict hard diffraction in  $pp$ :



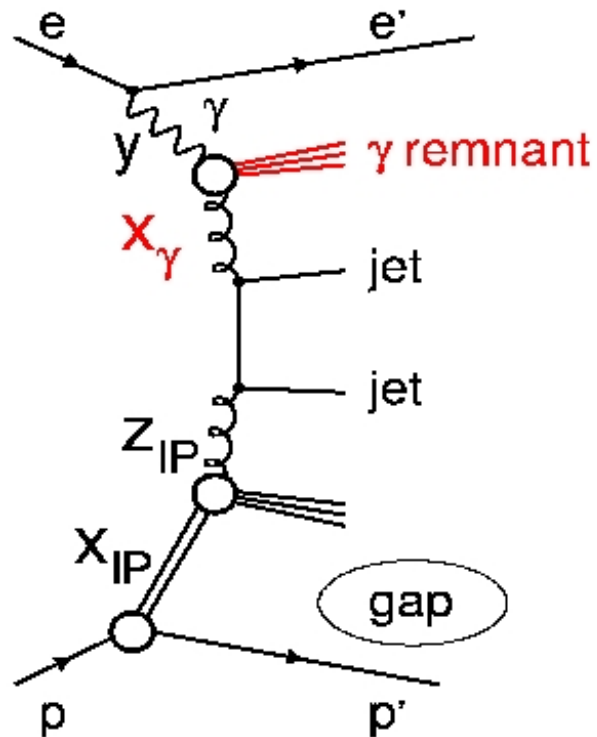
- Serious **breakdown of factorization** observed if HERA pdf's transported to TEVATRON:
- Prediction based on H1 pdf's **one order of magnitude above CDF data**
- Also observed for other processes:  
Relative rate of diffractive processes  $\sim 1\%$

Due to presence of second hadron in initial state?

Spectator interactions/rescattering effects break up  $\bar{p}$ , “rapidity gap survival probability”

## Dijets in Diffractive Photoproduction ( $Q^2 \sim 0$ )

Real photon  $\sim$  hadron: Look at HERA in photoproduction ...



Real photon may develop **hadronic structure**  
 $\rightarrow$  similar to hadron-hadron interactions

$x_\gamma$ : Momentum fraction of photon entering the hard process

- $x_\gamma = 1$ : Direct interaction, similar to DIS
- $x_\gamma < 1$ : Resolved interaction, similar to hadron-hadron scattering

- Does QCD factorization also work in diffractive photoproduction (although not proven)?
- Is there a dependence on  $x_\gamma$ ?
- Can factorization breaking w.r.t. Tevatron be understood?

## Dijets in Diffractive Photoproduction

H1 data:

$$Q^2 < 0.01 \text{ GeV}^2, 0.3 < y < 0.65$$

$$x_{\mathbb{P}} < 0.03$$

Jets: incl.  $k_T$  algo.

$$p_{T,1(2)} > 5(4) \text{ GeV}$$

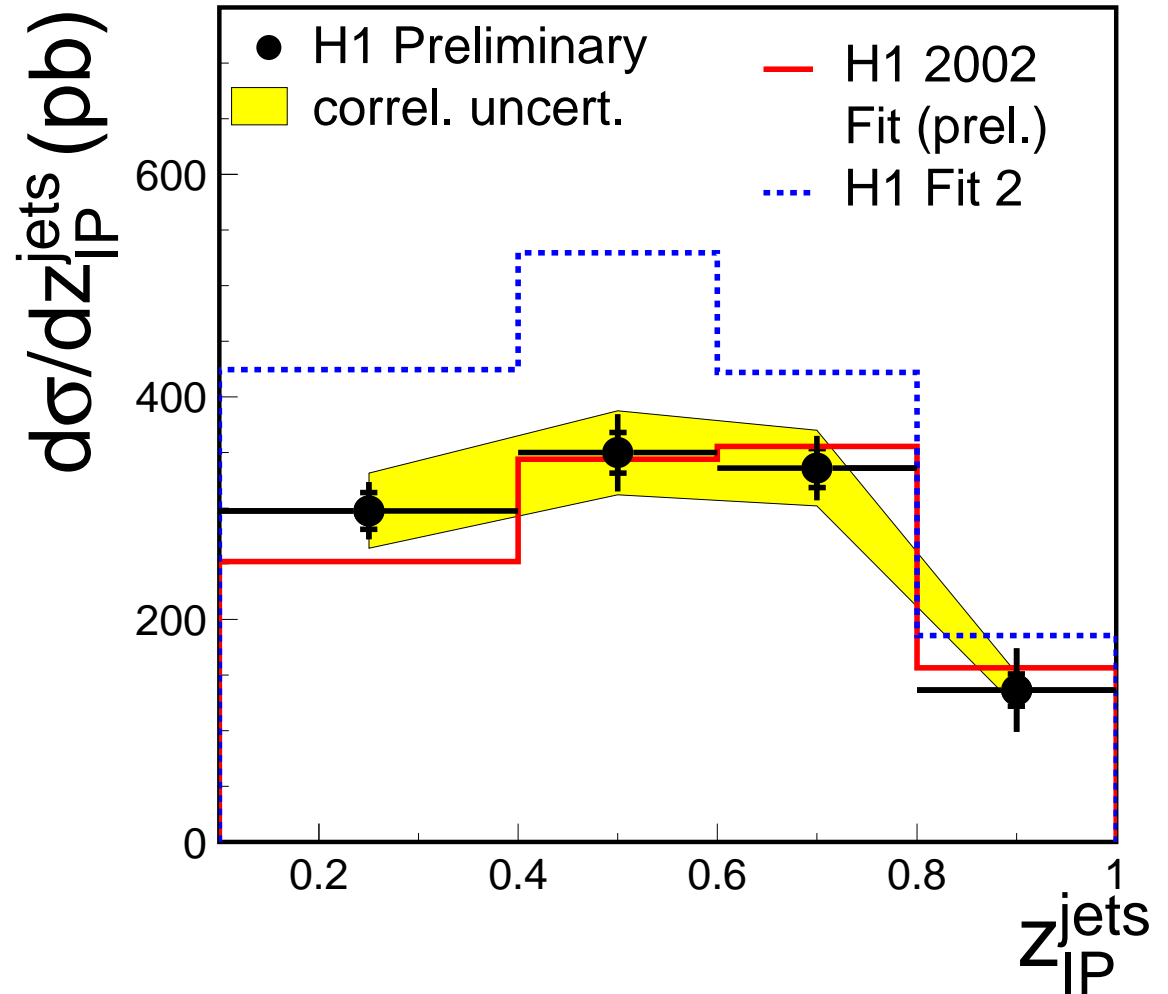
Monte Carlo comparisons:

LO ME + parton showers: RAPGAP

$$\mu_r^2 = p_T^2$$

- New 2002 LO fit describes data very well
- Old "H1 fit 2" too high, but large uncertainties

### H1 Diffractive $\gamma p$ Dijets



## Dijets in Diffractive Photoproduction

- Cross section as a function of  $x_\gamma$
- New 2002 fit describes direct and resolved contribution

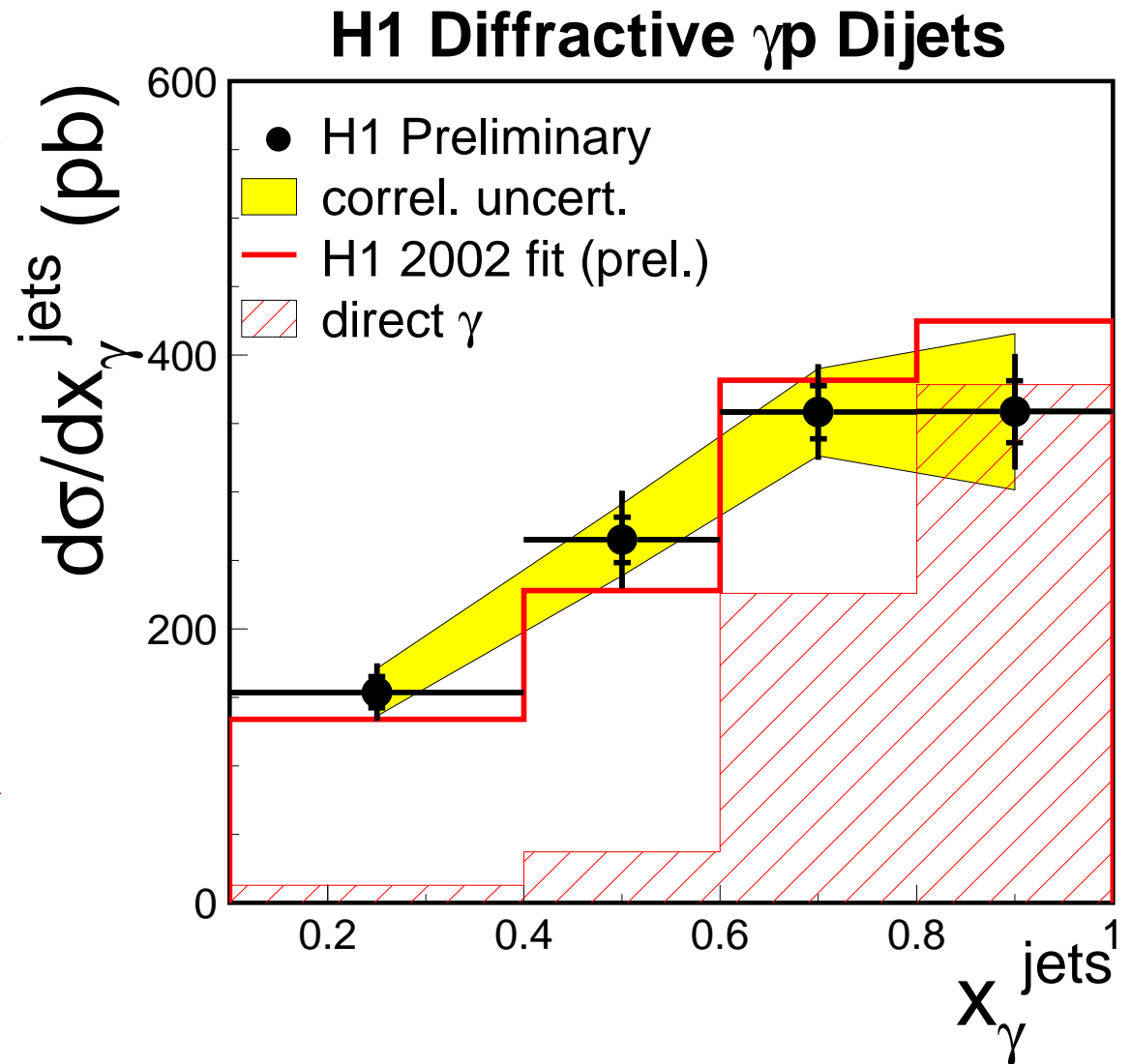
Direct comparison DIS vs  $\gamma p$ :

$$\frac{\left(\frac{Model}{Data}\right)_{\gamma p}}{\left(\frac{Model}{Data}\right)_{DIS}} = 1.25 \pm 0.30(\text{exp.})$$

Within uncertainties **no suppression** of  $\gamma p$  w.r.t. DIS diffractive jets

Independent of fit

(NLO Calculations being worked on...)





## Conclusions

### HERA-I has told us:

- Diffractive DIS at HERA: Investigate **quark/gluon structure of diffraction**
- **High precision HERA data** in large kinematic range available
- **Diffractive pdf's of proton** have been determined at NLO
- Comparison with jets/charm: **Self-consistent QCD picture of diffractive DIS to NLO**
- Does factorization also hold in diffractive photoproduction? (Need NLO calc.)

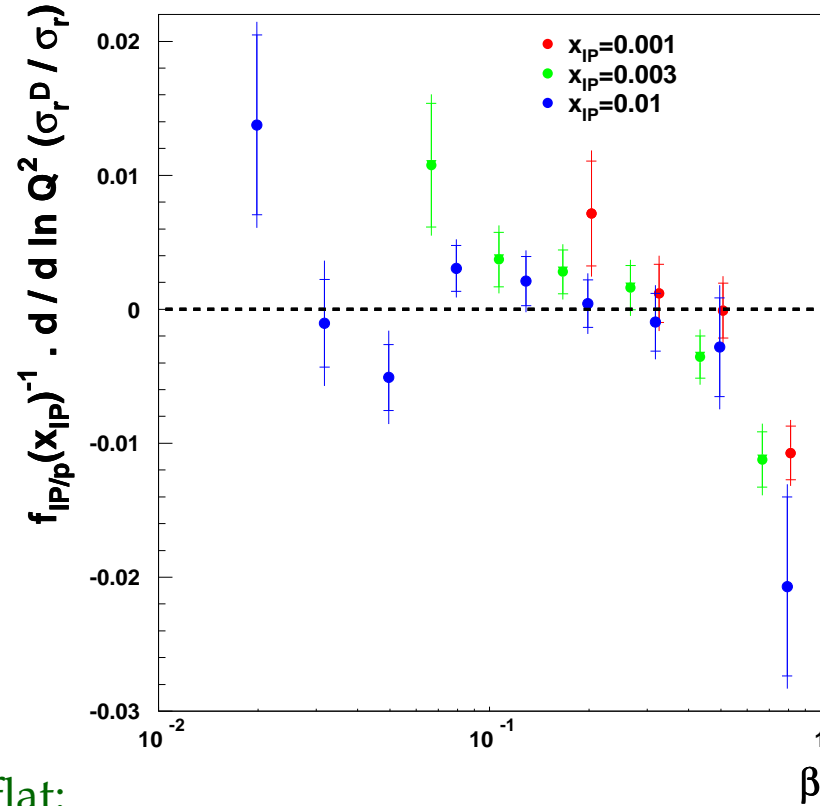
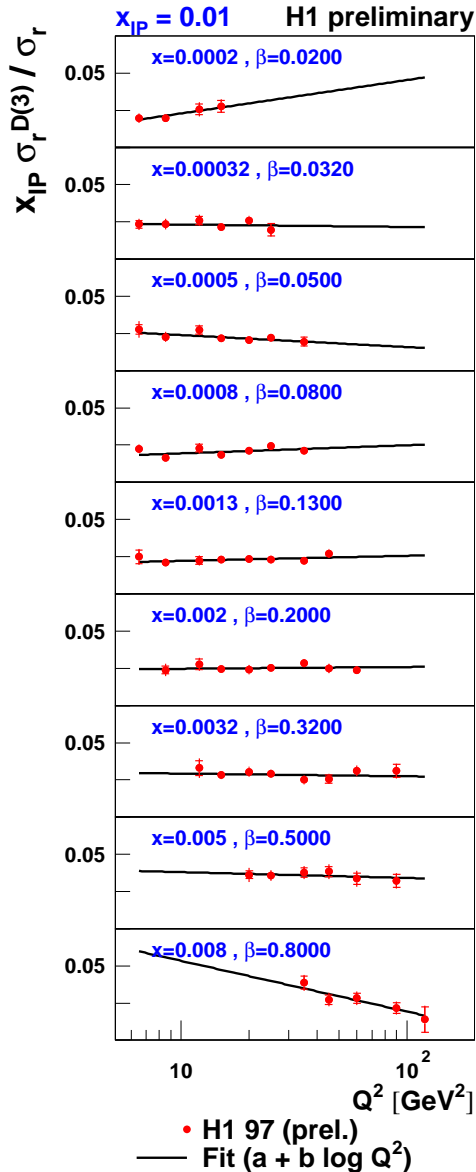
### From HERA to the LHC (via TEVATRON):

- HERA-II to provide a lot **more data**  
(in particular using the H1 VFPS)
- Understanding of **factorization breaking mechanism**  $ep$  vs  $pp$  needed
- Need diffr. pdf's in **kinematic range relevant for LHC!**
- Can **diffractive pdf's + non-factorizing mechanism** be combined in a sensible way to obtain predictions for the LHC (e.g. diffractive Higgs)?

# BACKUP

# Ratio Diffractive / Inclusive: $Q^2$ dependence (H1)

Logarithmic  $Q^2$  dependence of the ratio  $\left. \frac{\sigma_r^{D(3)}(x, Q^2, x_{IP})}{\sigma_r(x, Q^2)} \right|_{x, x_{IP}} \sim A_R + B_R \log Q^2$

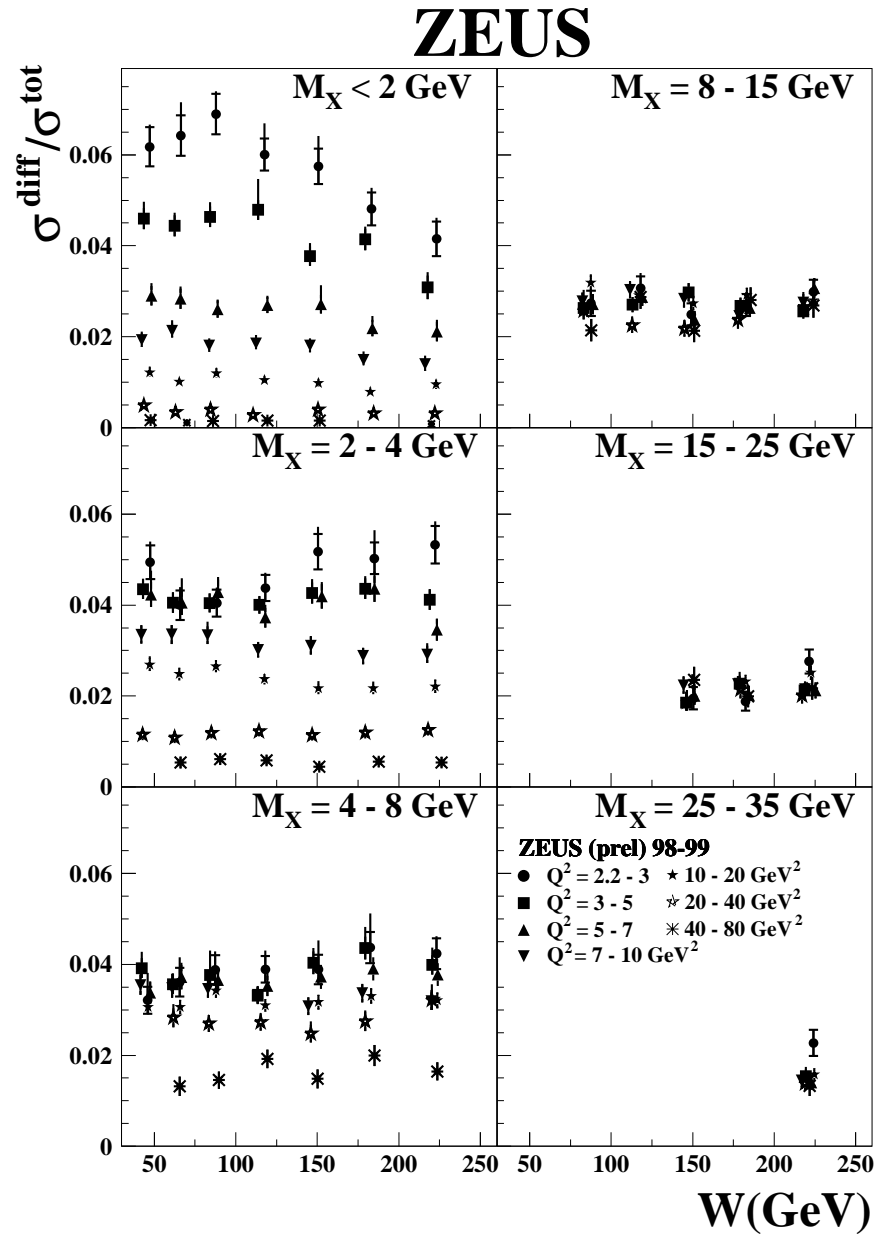


Low  $\beta$ : rel. flat:

- ratio of diffr. to incl.  $g(x, Q^2)$  constant
- dipole models (IF  $\sigma_{dipole} \propto R$ )

As  $\beta = 1$ : falling:

- $Q^2$ -suppressed higher twist (pert. 2-gluon exchange)
- DGLAP evolution (gluon radiation)



## Diffractive / Inclusive: Ratio from ZEUS

Similar features observed:

- little  $Q^2$  dependence at high  $M_X$   
( $\sim$  low  $\beta$ )
- strong (negative)  $Q^2$  dependence  
at small  $M_X$   
( $\sim$  high  $\beta$ )