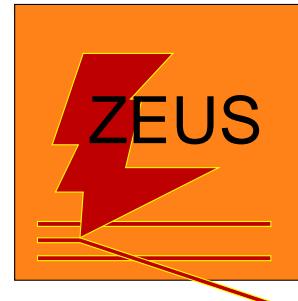


# Inclusive Diffraction at HERA: Diffractive pdf's and QCD factorization tests

Frank-Peter Schilling

[DESY]



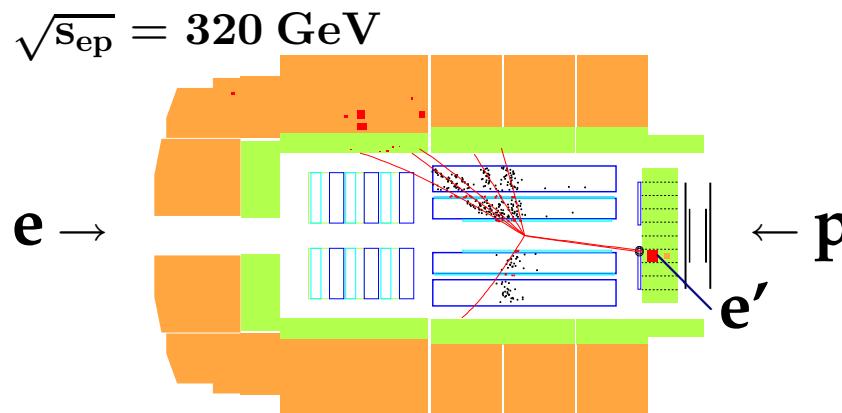
## Contents:

- QCD factorization in diffraction
- Inclusive Diffractive DIS
- Determination of diffractive pdf's
- Factorization tests with jets and charm  
(HERA, Tevatron)

Diffraction at the LHC  
Rio de Janeiro, April 2004

# Diffraction at HERA

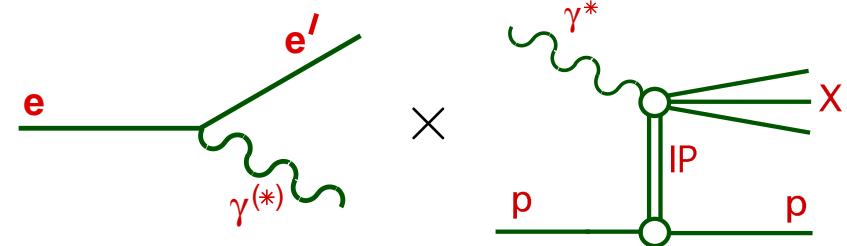
- HERA: An ideal laboratory to study **hard diffraction**:
- 10% of low- $x$  DIS events are diffractive



**Virtual photon  $\gamma^*$  as a probe**

- Inclusive DIS:  
Probe proton structure ( $F_2(x, Q^2)$ )
- Diffractive DIS:  
Probe structure of  
colour singlet exchange!

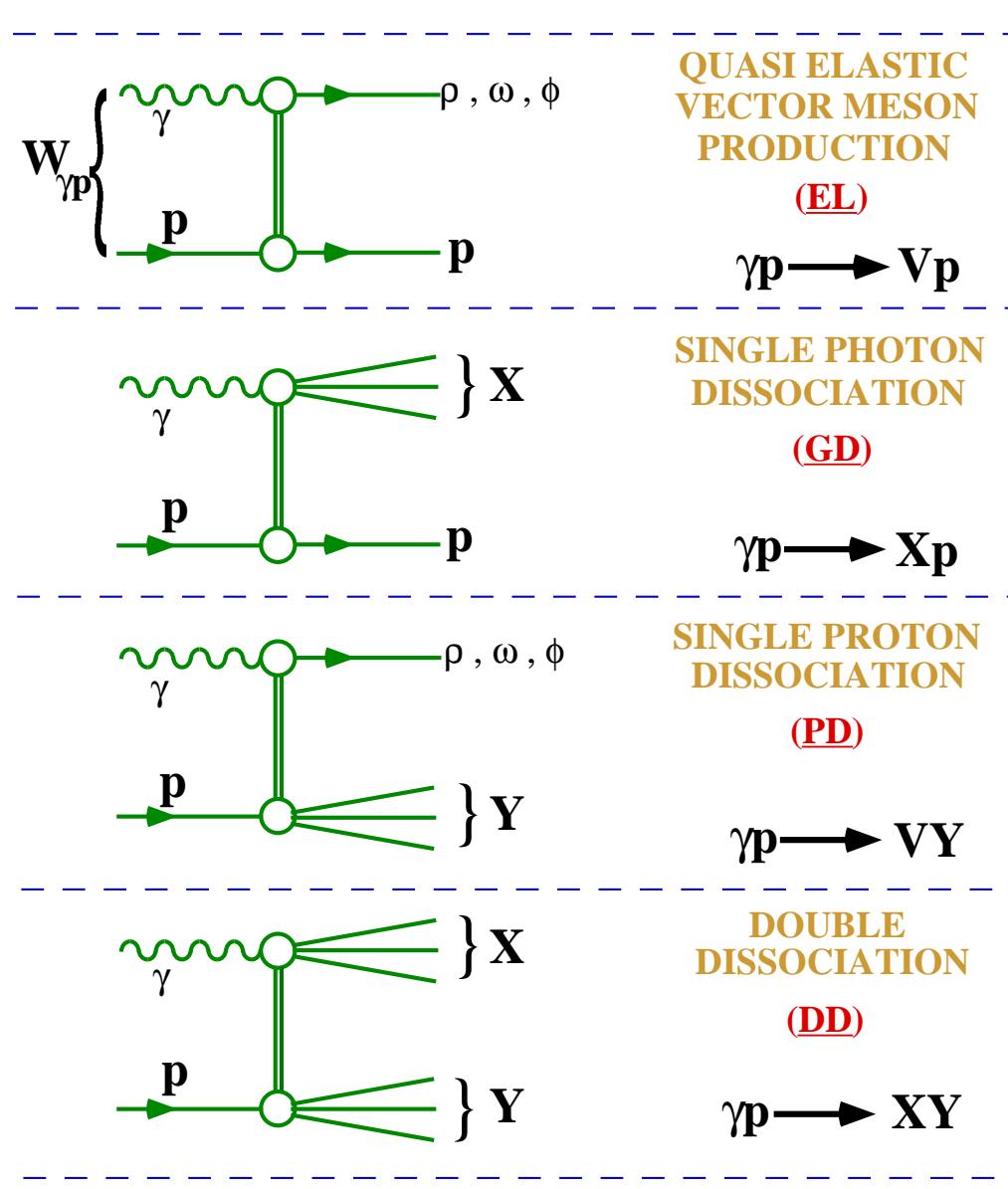
Can be viewed as diffractive  
 $\gamma^* p$  interaction:



Why diffraction?

- Diffraction is significant part of  $\sigma_{\text{tot}}$
- Novel tool to study **soft-hard transition in QCD**
- **Low- $x$  structure of the proton**  
(e.g. saturation)

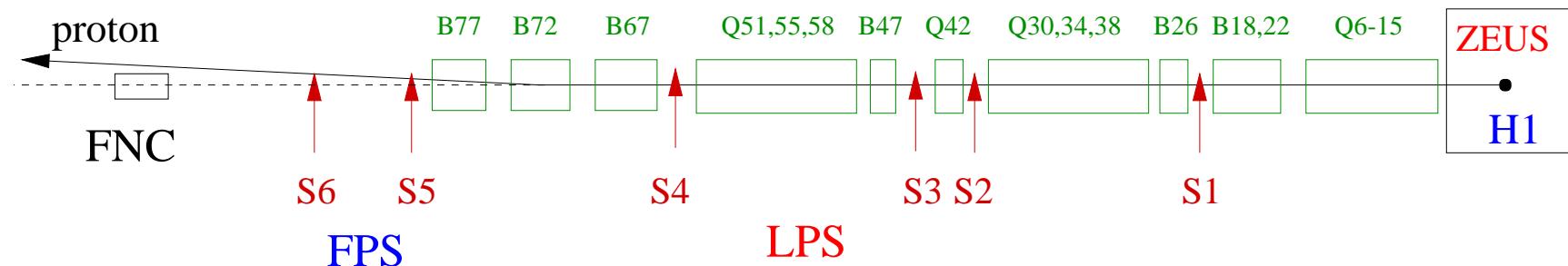
## Diffractive Processes in $\gamma p$ Interactions



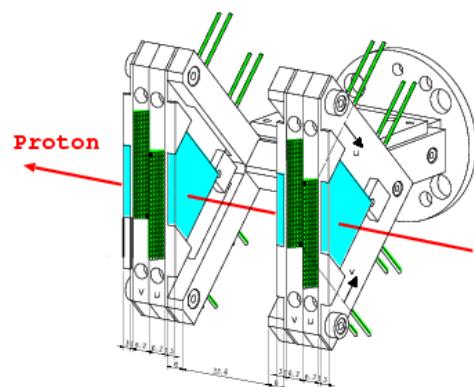
- All 4 processes can be measured with varying  $Q^2, W, t, M_X, M_Y$
- large  $Q^2$ :  
 $\gamma^*$  probes diffractive exchange  
This talk!
- large  $|t|$ : perturbative QCD applicable to  $IP$  (BFKL)?
- $Q^2 \sim 0, |t| \sim 0$ : similar to soft hadronic diffraction

Exclusive diffraction (VM, DVCS, ...):  
see talk by Mara Soares!

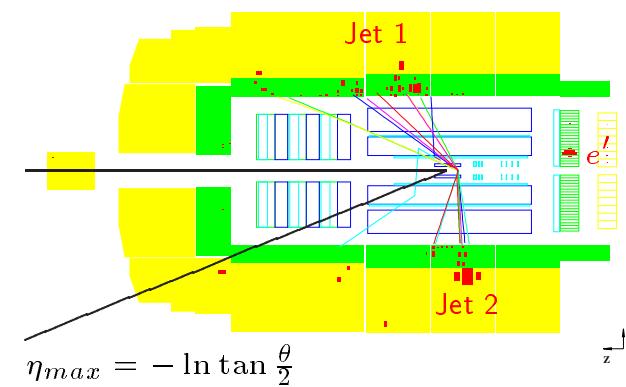
## Experimental Techniques



Forward Proton Spectrometers  
at  $z = 24\ldots90$  m



Rapidity Gap Selection  
in central detector



### Measure leading proton

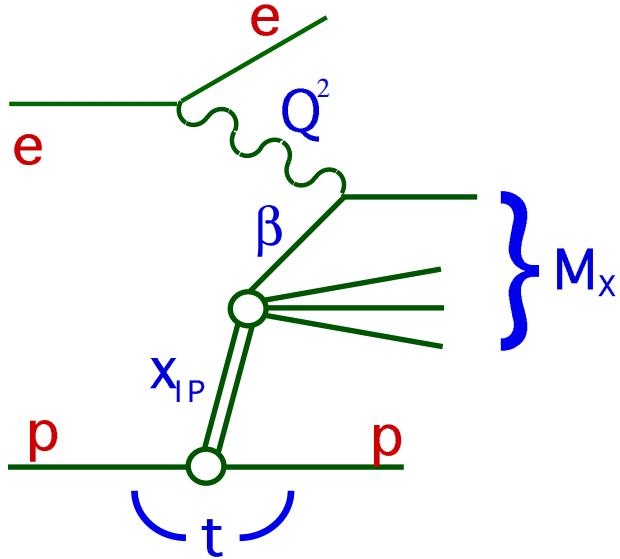
- Free of dissociation bkgd.
- Measure  $p$  4-momentum
- low statistics (acceptance)

### Require large rapidity gap

- $\Delta\eta$  large when  $M_{\text{central}} \ll W_{\gamma p}$
- integrate over outgoing  $p$  system
- high statistics (similar:  $M_X$  method)

## Diffractive Cross section and Structure Functions

In a frame where the proton is moving fast:



$$x_{IP} = \xi = \frac{Q^2 + M_X^2}{Q^2 + W^2} = x_{IP}/p$$

(momentum fraction of colour singlet exchange)

$$\beta = \frac{Q^2}{Q^2 + M_X^2} = x_q/IP$$

(fraction of exchange momentum of  
q coupling to  $\gamma^*$ ,  $x = x_{IP}\beta$ )

$$t = (p - p')^2$$

(4-momentum transfer squared)

Diffractive reduced cross section  $\sigma_r^D$ :

$$\frac{d^4\sigma}{dx_{IP} dt d\beta dQ^2} = \frac{4\pi\alpha^2}{\beta Q^4} \left(1 - y + \frac{y^2}{2}\right) \sigma_r^{D(4)}(x_{IP}, t, \beta, Q^2)$$

Structure functions  $F_2^D$  and  $F_L^D$ :

$$\sigma_r^{D(4)} = F_2^{D(4)} - \frac{y^2}{2(1-y+y^2/2)} F_L^{D(4)}$$

Integrated over  $t$ :  $F_2^{D(3)} = \int dt F_2^{D(4)}$

- Longitudinal  $F_L^D$ : affects  $\sigma_r^D$  at high  $y$
- If  $F_L^D = 0$ :  $\sigma_r^D = F_2^D$

[ $\gamma$  inelasticity  $y = Q^2/sx$ ]

## Factorization in Diffraction

Diffractive pdf's / proof of QCD Factorization for diffractive DIS:

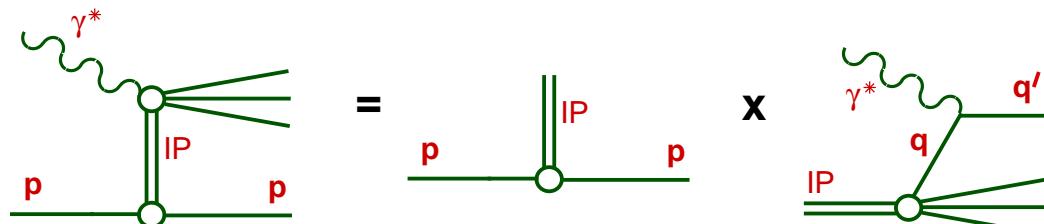
- Diffractive parton distributions (Trentadue, Veneziano, Berera, Soper, Collins, ...):

$$\frac{d^2\sigma(x, Q^2, x_{IP}, t) \gamma^* p \rightarrow p' X}{dx_{IP} dt} = \sum_i \int_x^{x_{IP}} d\xi \hat{\sigma}^{\gamma^* i}(x, Q^2, \xi) p_i^D(\xi, Q^2, x_{IP}, t) \quad (+\text{higher twist})$$

- $\hat{\sigma}^{\gamma^* i}$  hard scattering coeff. functions, as in incl. DIS
- $p_i^D$  diffractive PDF's in proton, conditional probabilities, valid at fixed  $x_{IP}, t$ , obey (NLO) DGLAP

Ingelman-Schlein Model ('Resolved Pomeron' model):

$x_{IP}, t$  dependence factorizes out (Donnachie, Landshoff, Ingelman, Schlein, ...):

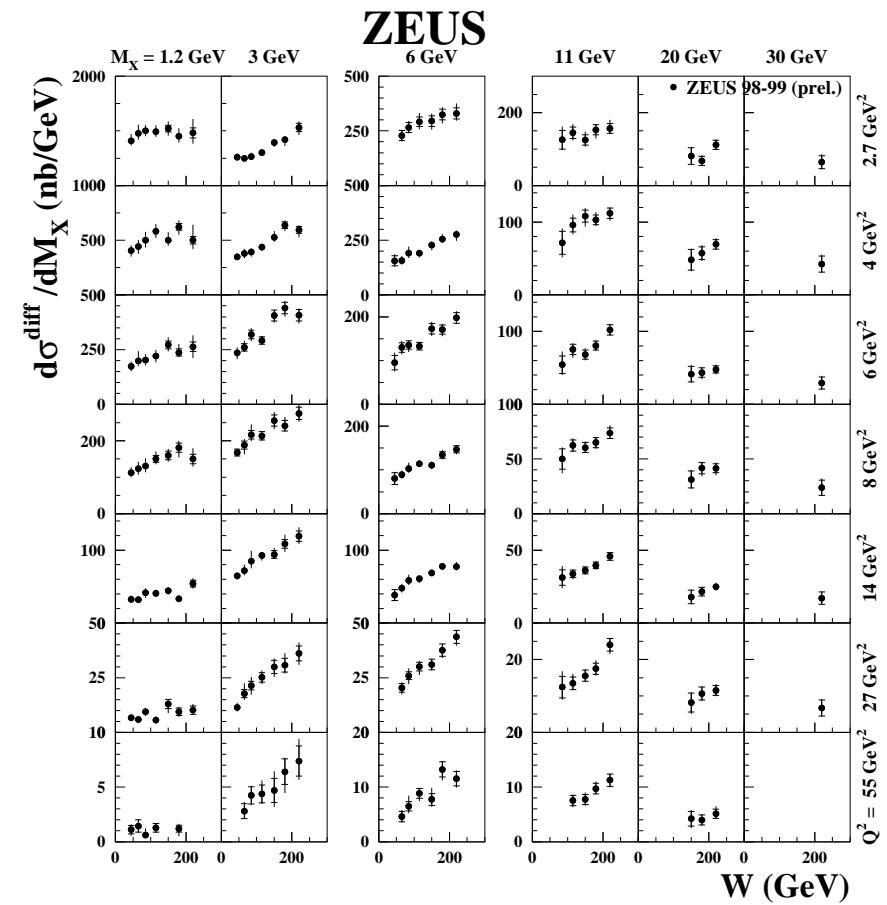
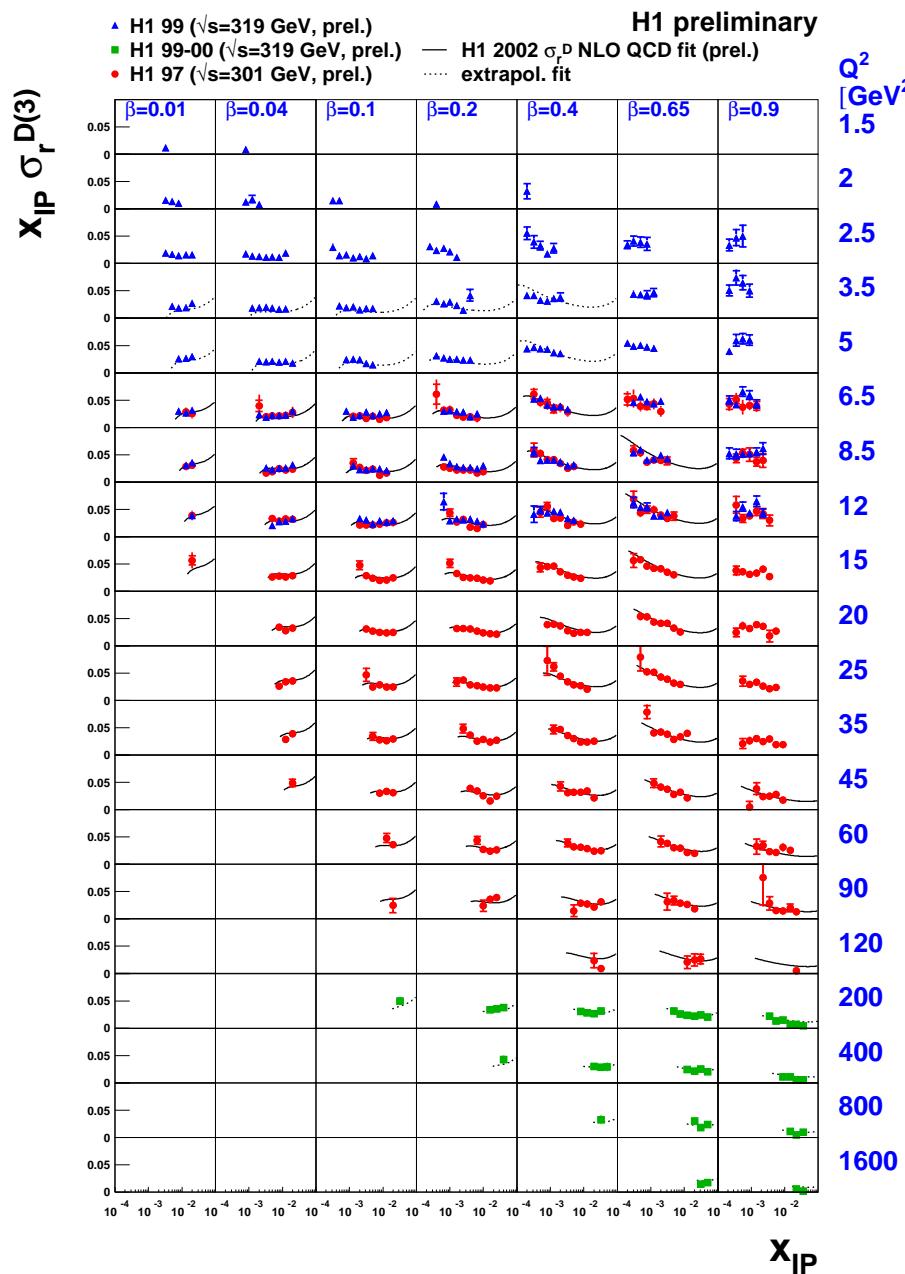


$$F_2^D(x_{IP}, t, \beta, Q^2) = f_{IP/p}(x_{IP}, t) F_2^{IP}(\beta, Q^2)$$

- additional assumption, no proof !
- consistent with present data if sub-leading IR included

Shape of diffr. PDF's indep. of  $x_{IP}, t$ , normalization controlled by Regge flux  $f_{IP/p}$

# Recent Diffractive DIS cross section data



- Large kinematic range covered
  - $1.5 < Q^2 < 1600 \text{ GeV}^2$
  - large stat. precision
  - At low  $Q^2$  limited by syst. err. from diffractive selection

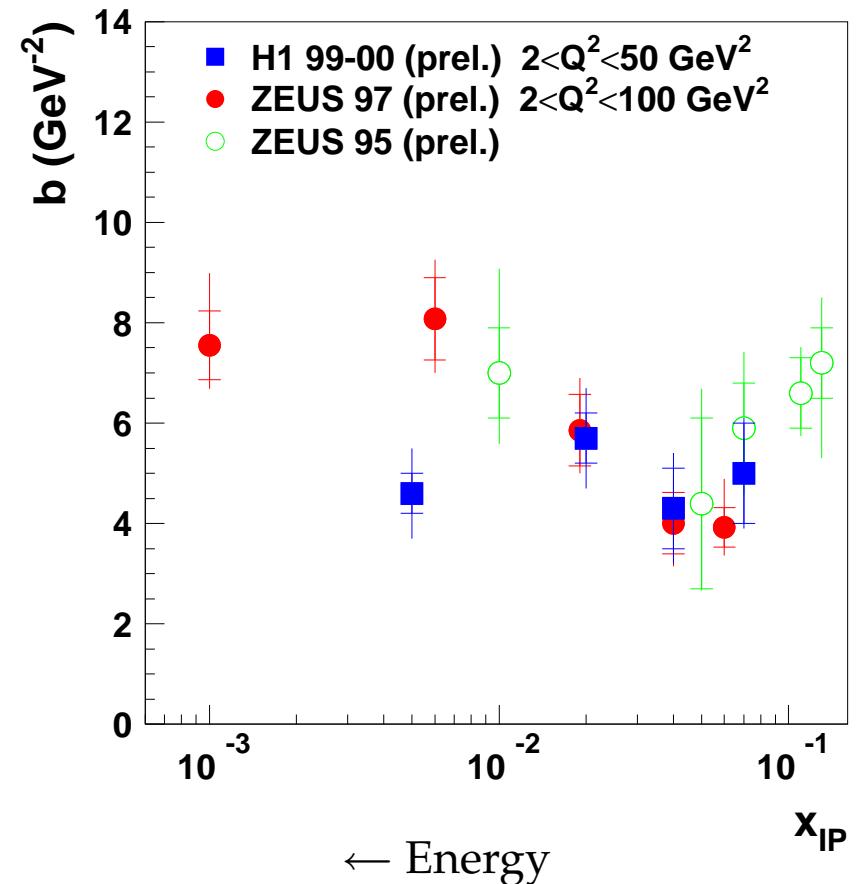
## Forward Proton Detectors: $t$ Measurement

$\frac{d\sigma}{d|t|}$  measured for  $-0.4 \lesssim t < |t|_{\min}$

Exponential fit to  $t$  distribution:

$$\frac{d\sigma}{d|t|} \sim e^{-b|t|}$$

$b$  is related to  
the interaction radius:  $b = R^2/4$



In Regge phenomenology expect 'shrinkage':  
(proton gets 'bigger' with increasing energy)

$$b = b_0 + 2\alpha' \log \frac{1}{x_{IP}} \quad x_{IP} \sim M_X^2/W_{\gamma p}^2$$

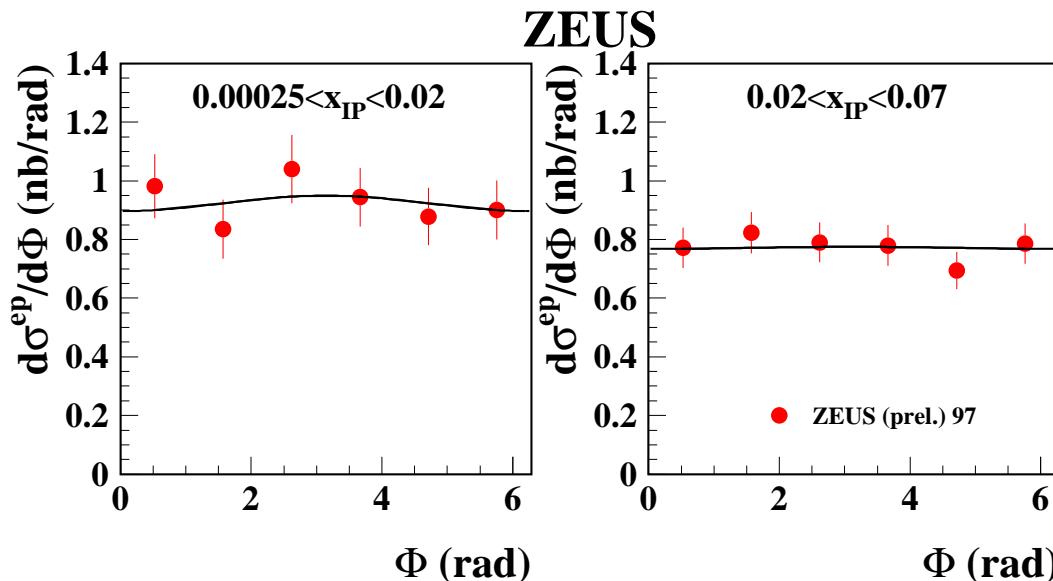
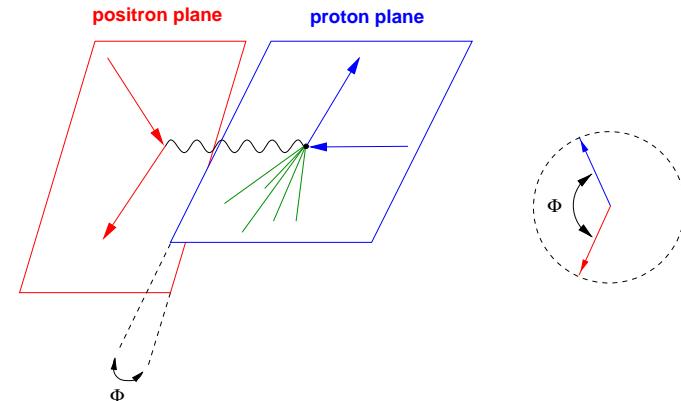
So far inconclusive ...

## Forward Proton Detectors: $\phi$ Measurement

$\Phi$ : Azimuthal angle between electron and proton scattering planes

$\frac{d\sigma^D}{d\Phi}$  sensitive to  $\sigma_L^D$  through interf. term:

$$\frac{d\sigma^D}{d\Phi} \sim \sigma_T^D + \epsilon \sigma_L^D - 2\sqrt{\epsilon(1+\epsilon)} \sigma_{LT}^D \cos \Phi - \epsilon \sigma_{TT}^D \cos 2\Phi$$



Measured asymmetries  
from fit  $\frac{d\sigma}{d\Phi} \sim 1 + A_{LT} \cos \Phi$ :

$$A_{LT} = -0.029 \pm 0.066^{+0.026}_{-0.047} \quad (0 \lesssim x_{IP} < 0.02 ; \beta \approx 0.32)$$

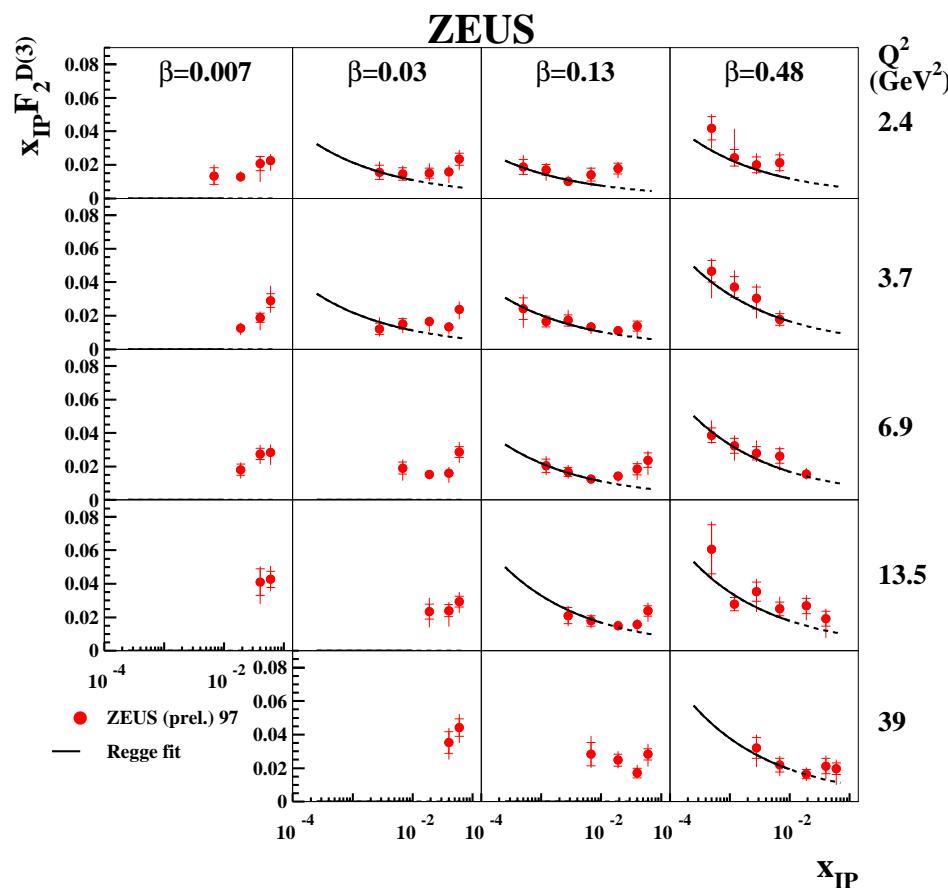
$$A_{LT} = -0.005 \pm 0.052^{+0.048}_{-0.047} \quad (0.02 < x_{IP} < 0.07 ; \beta \approx 0.1)$$

⇒ Interference term small in measured region

[Interesting high  $\beta$  region (pert. 2-gluon exch. predicts large asymmetry) not yet explored]

## Energy dependence and $\alpha_{IP}(0)$

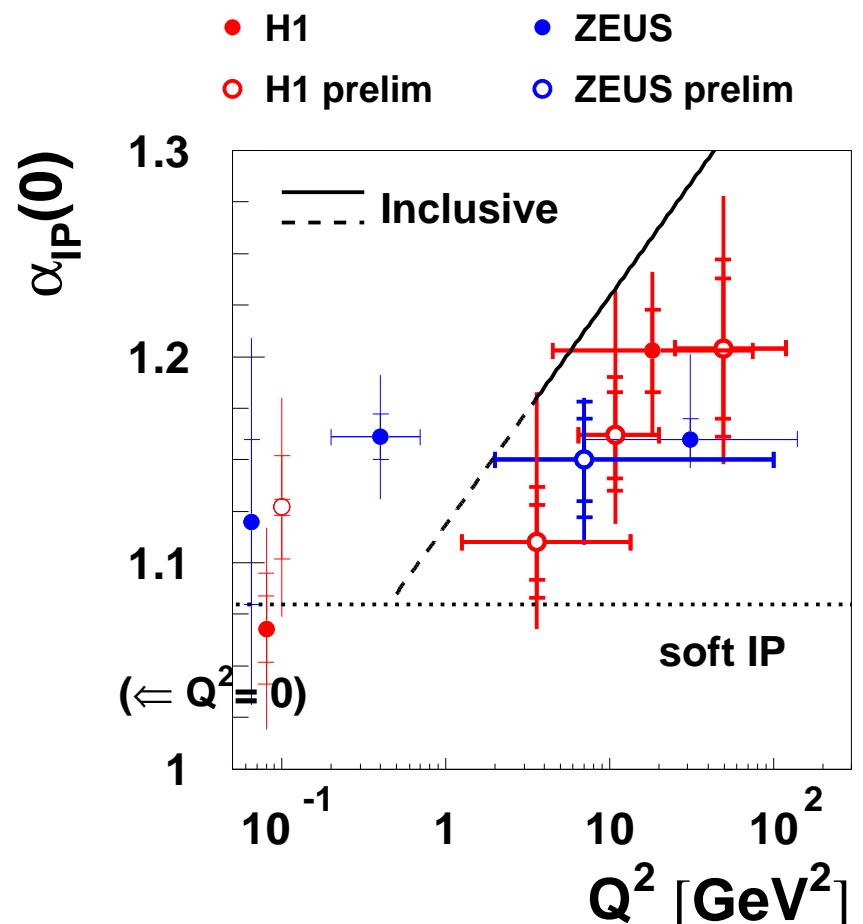
Example: ZEUS LPS data



Fit to  $x_{IP}$  dependence:

$$F_2^D(x_{IP}, \beta, Q^2) = \left(\frac{1}{x_{IP}}\right)^{2\overline{\alpha}_{IP}-1} \cdot A(\beta, Q^2)$$

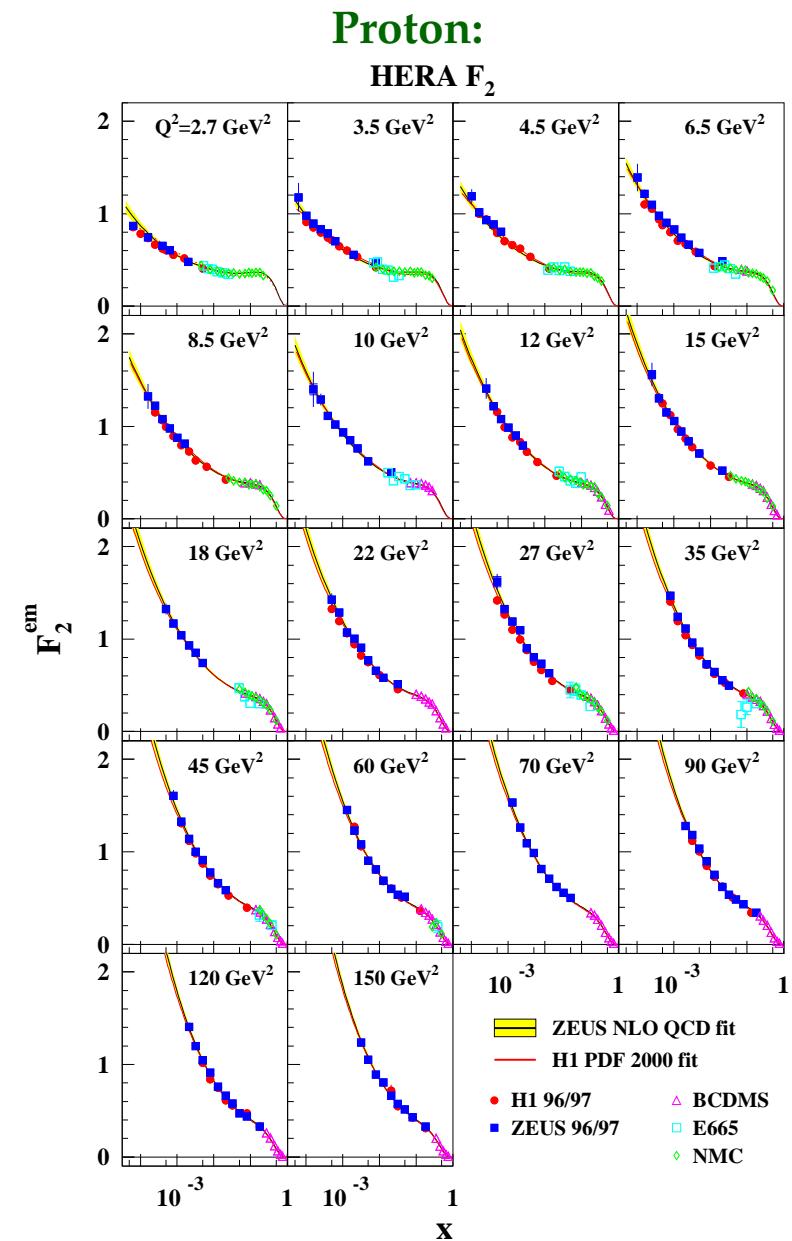
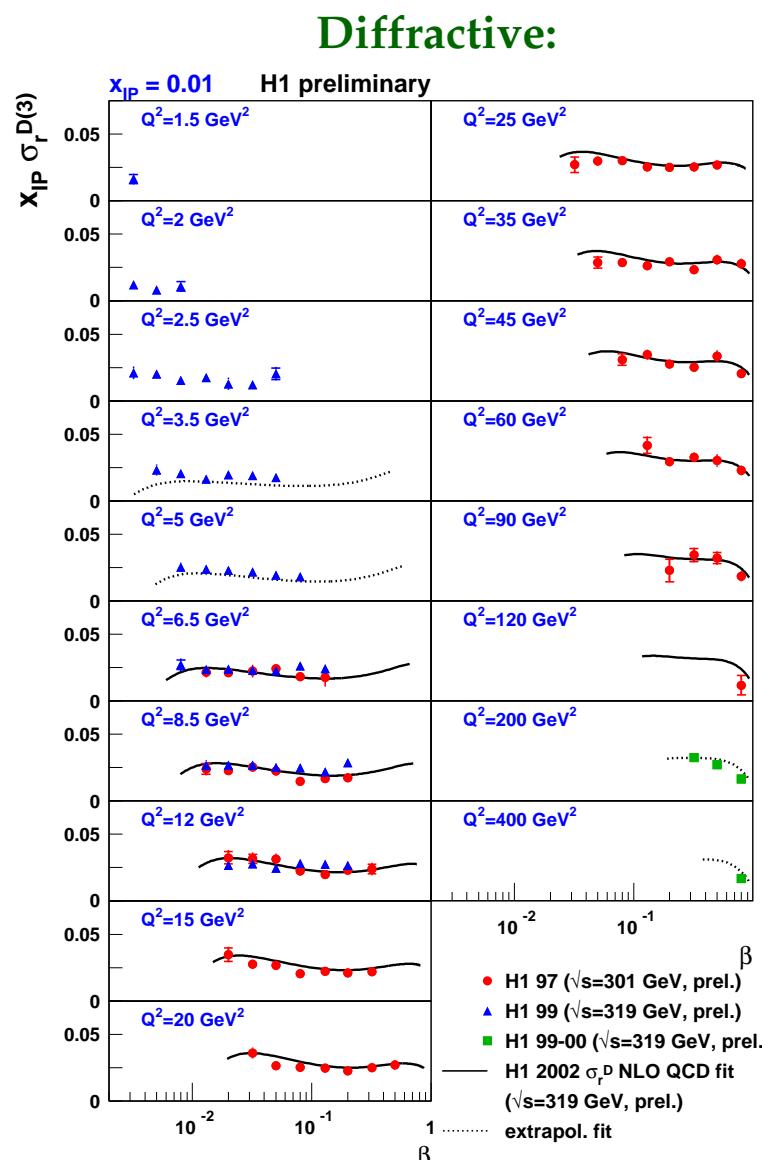
## Diffractive effective $\alpha_{IP}(0)$



Indications for increase with  $Q^2$ ?

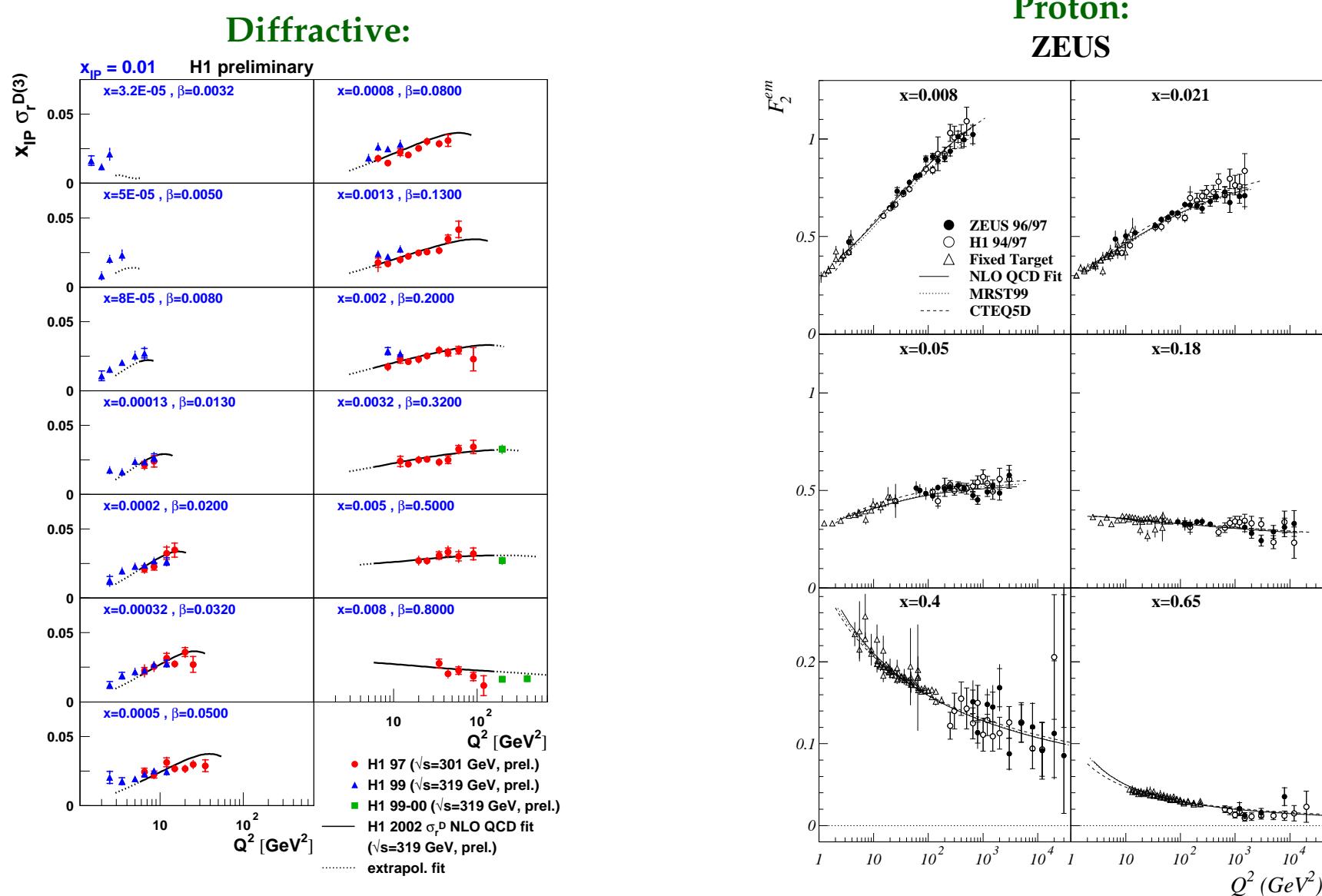
Naive expectation  $\alpha_{IP}^{\text{diff.}}(0) = 2 \alpha_{IP}^{\text{inc}}(0)$  fails in DIS region?

## Comparision diffractive vs inclusive: $\beta$ or $x$ dependence



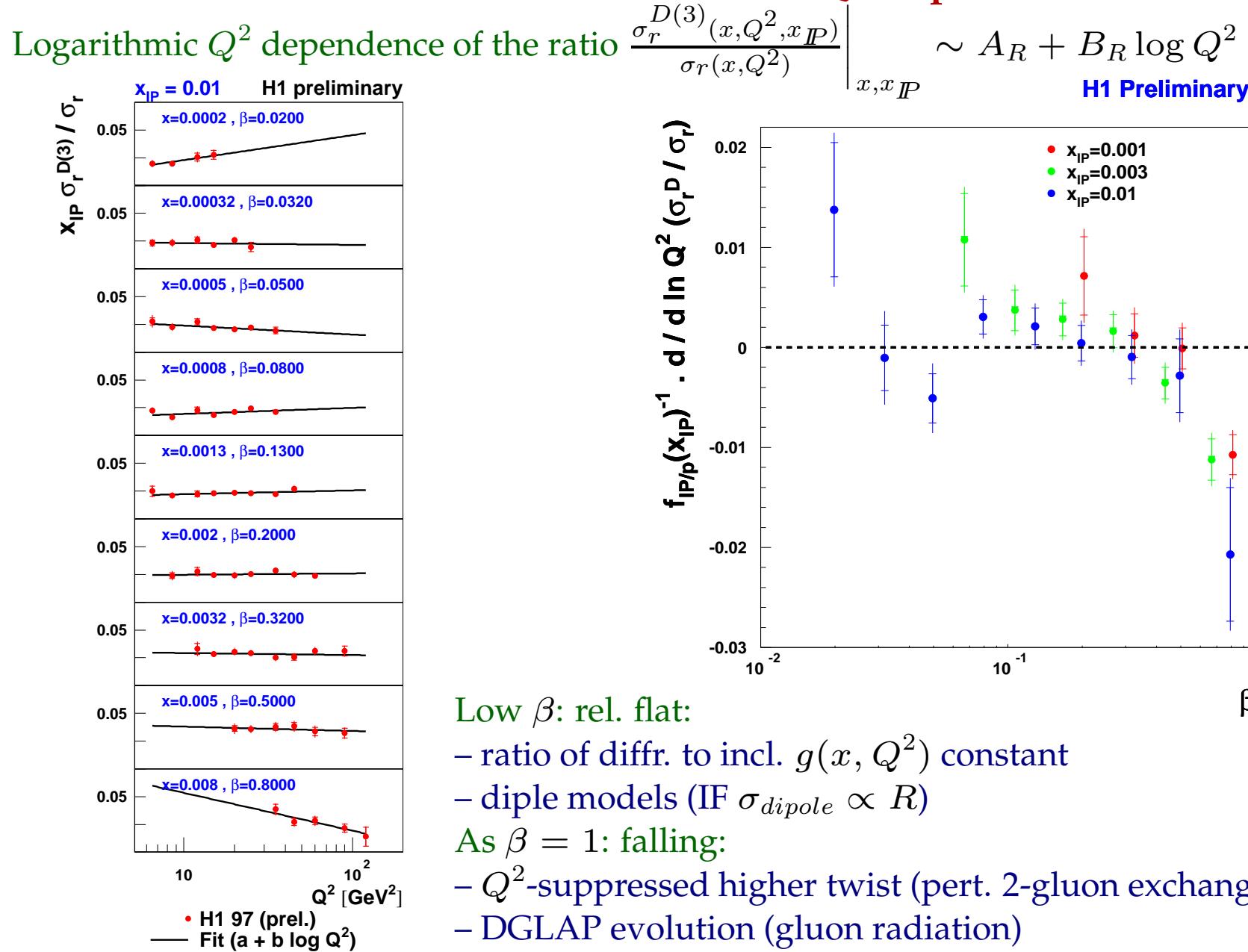
⇒ Only weak  $\beta$  dependence! Similar to photon ...

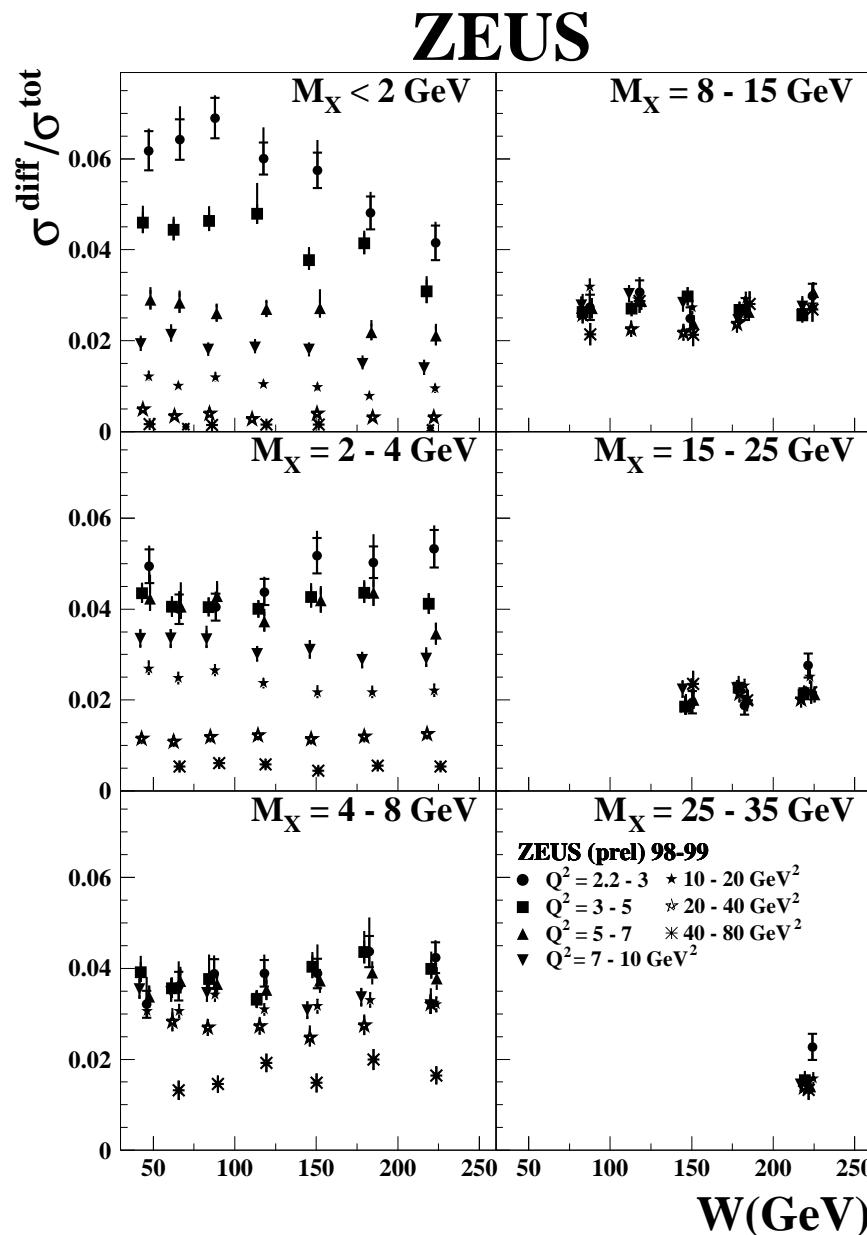
## Comparision diffractive vs inclusive: $Q^2$ dependence



$\Rightarrow +ve$  scaling violations to highest  $\beta$ : Gluon dominated!

## Ratio Diffractive / Inclusive: Q<sup>2</sup> dependence (H1)





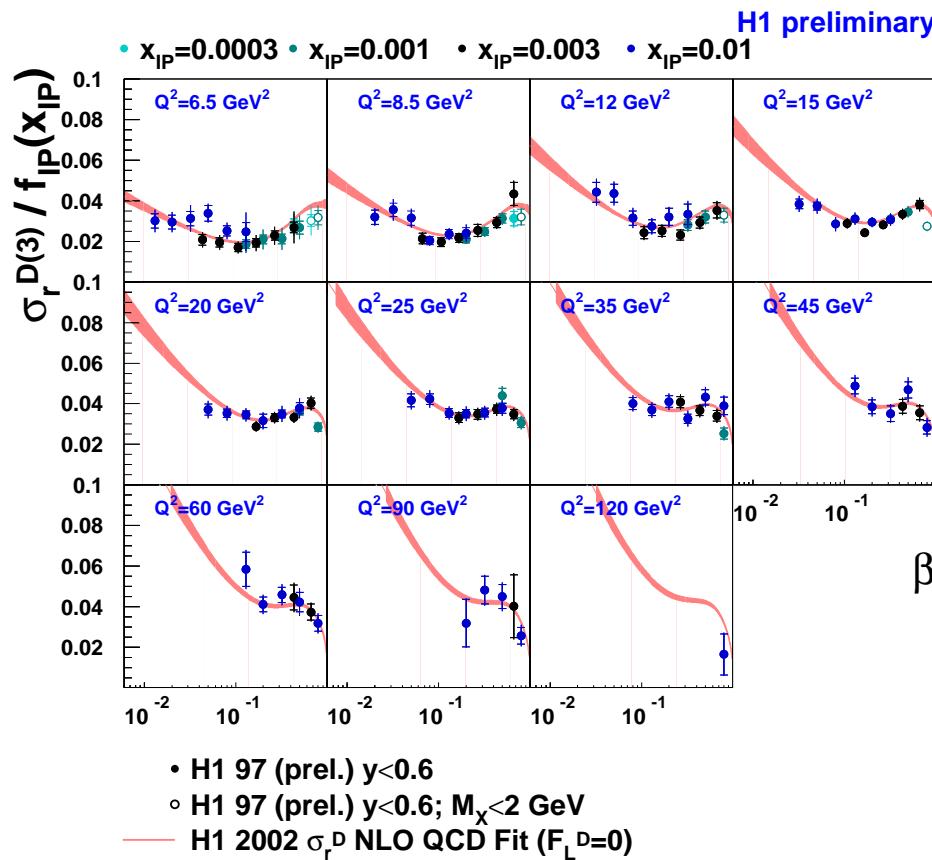
## Diffractive / Inclusive: Ratio from ZEUS

Similar features observed:

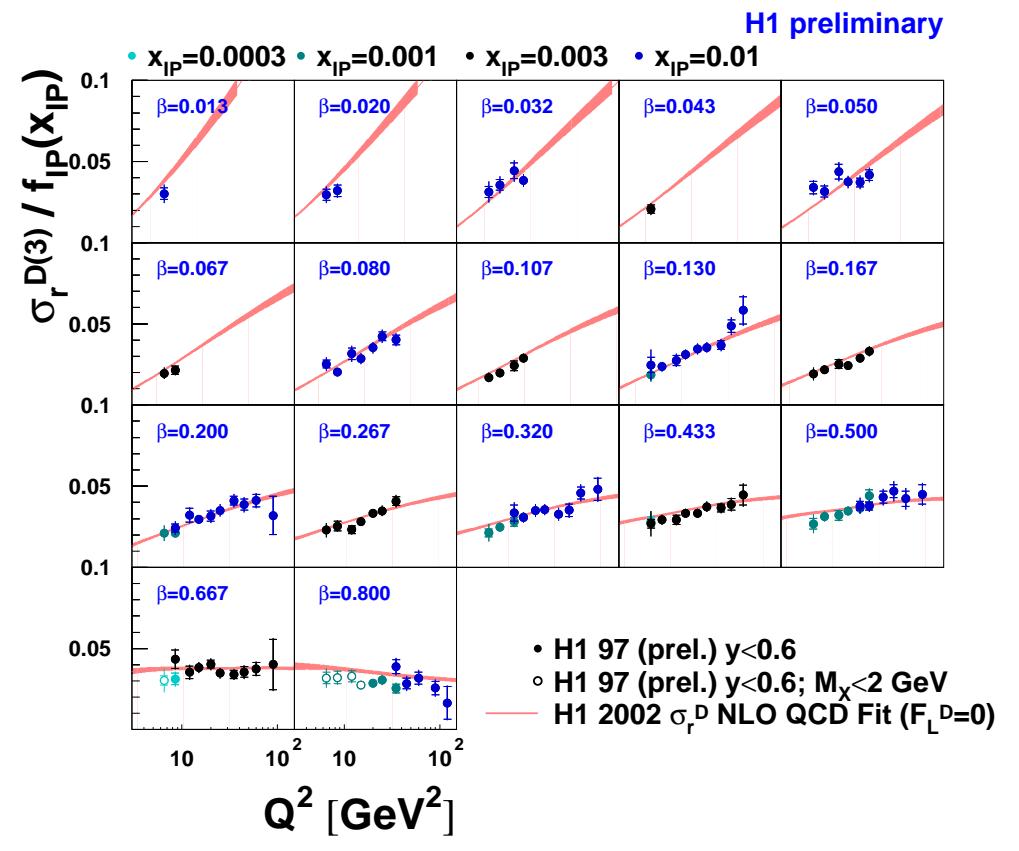
- little  $Q^2$  dependence at high  $M_X$  ( $\sim$  low  $\beta$ )
- strong (negative)  $Q^2$  dependence at small  $M_X$  ( $\sim$  high  $\beta$ )

## Precise H1 Measurement of $\beta, Q^2$ dependences

Prerequisite for NLO DGLAP QCD fit:



$$\beta \text{ dep.: } \sim \sum_i e_i^2 (q_i^D + \bar{q}_i^D)$$



$$d\sigma/d \ln Q^2: \sim \alpha_s \otimes g^D(\beta, Q^2)$$

- $x_{IP}$  dep. taken out: factorization holds for  $x_{IP} < 0.01$
- rising for  $\beta \rightarrow 1$  at low  $Q^2$
- positive scaling violations expect for largest  $\beta$  (gluon dominance)

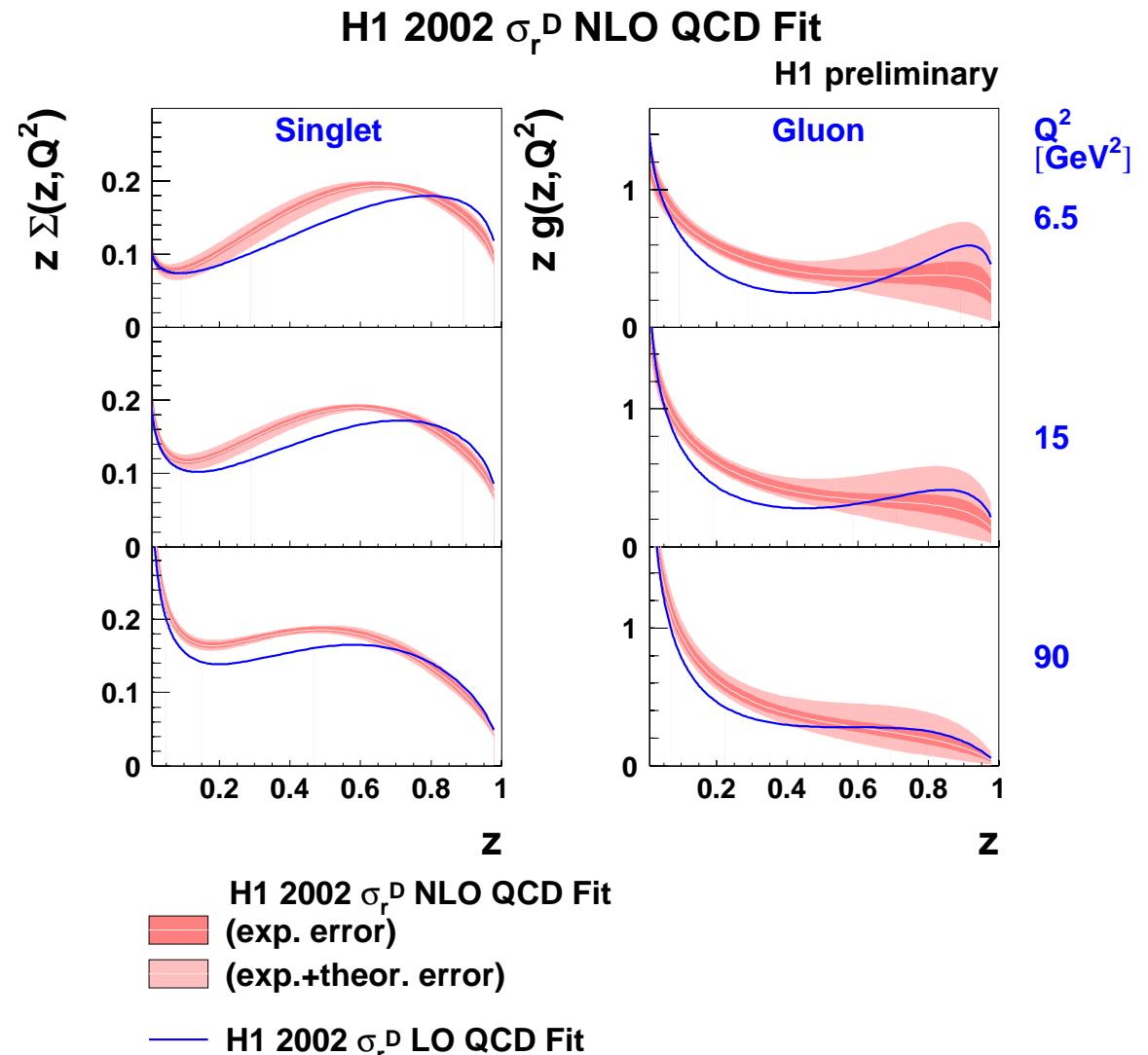
## NLO DGLAP QCD Fit (H1)

### QCD Fit Technique:

- factorize  $f(x_{IP})f(z, Q^2)$
- Singlet  $\Sigma$  and gluon  $g$  parameterized at  $Q_0^2 = 3 \text{ GeV}^2$
- NLO DGLAP evolution
- Fit data for  $Q^2 > 6.5 \text{ GeV}^2, M_X > 2 \text{ GeV}$
- For first time propagate exp. and theor. uncertainties !

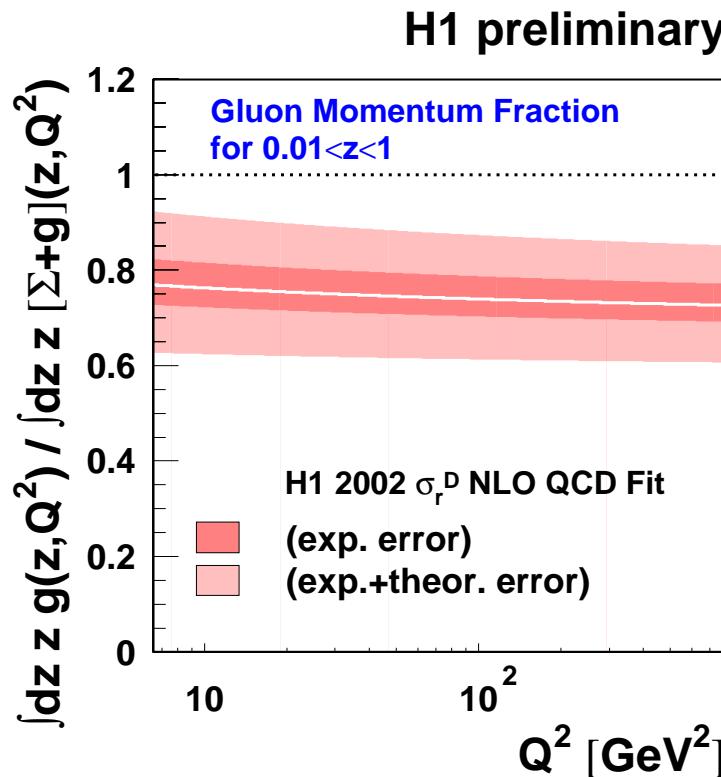
### PDF's of diffractive exchange:

- Extending to large fractional momenta  $z$
- Gluon dominated
- $\Sigma$  well constrained
- substantial uncertainty for gluon at highest  $z$
- Similar to previous fits



## H1 NLO QCD Fit: Gluon fraction and $F_L^D$

Integrate PDF's over measured range:

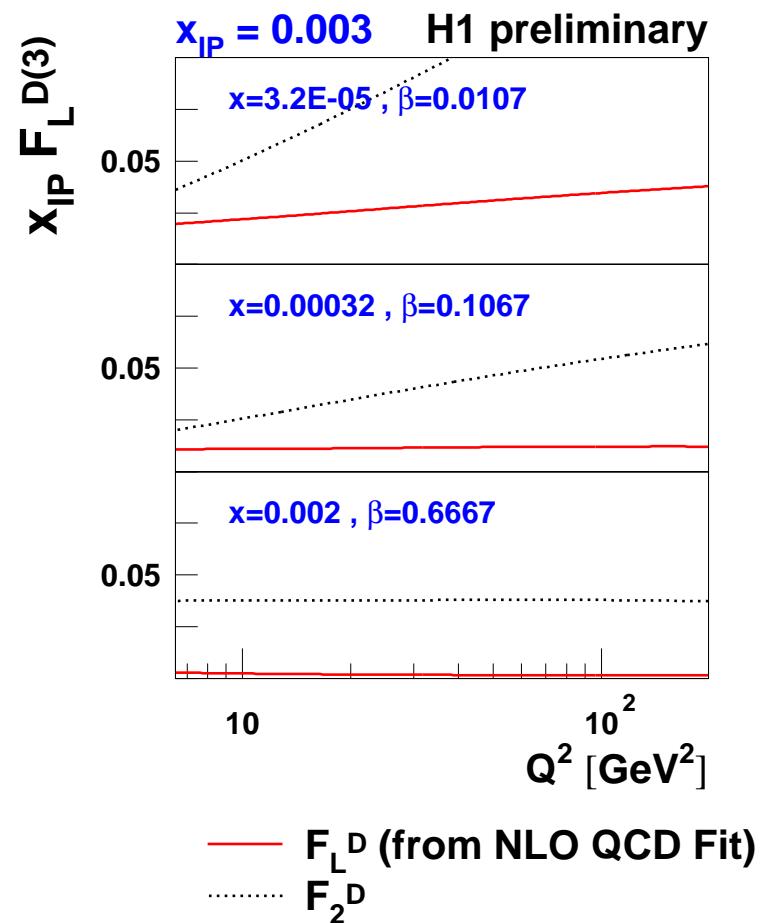


Momentum fraction of diffractive exchange carried by gluons:

$$75 \pm 15\%$$

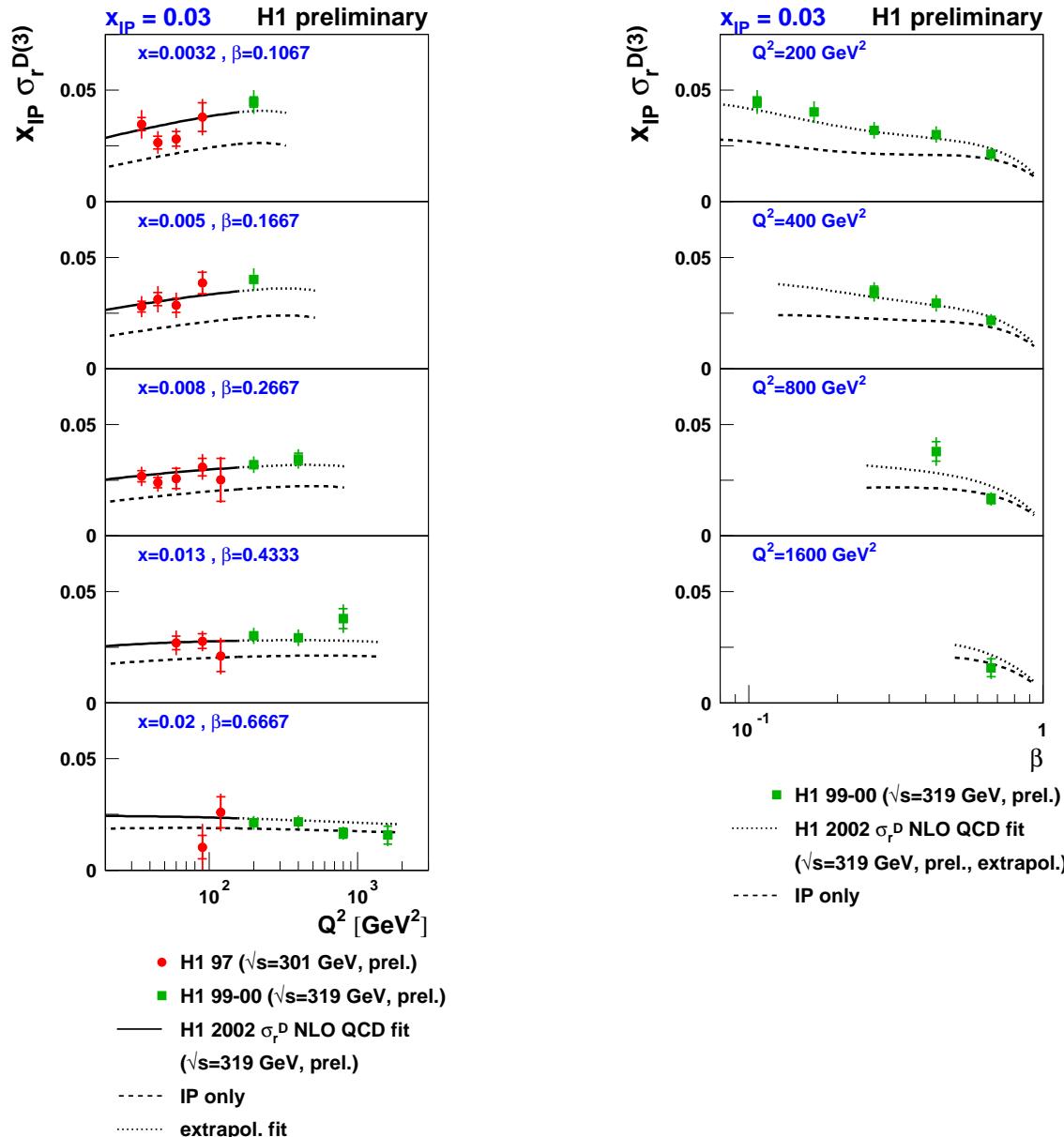
Longitudinal  $F_L^D$ :

$$F_L^D \sim \frac{\alpha_s}{2\pi} \left[ C_q^L \otimes F_2^D + C_g^L \otimes \sum_i e_i^2 z g^D(z, Q^2) \right]$$



$\Rightarrow F_L^D$  large at low  $Q^2$ , low  $\beta$

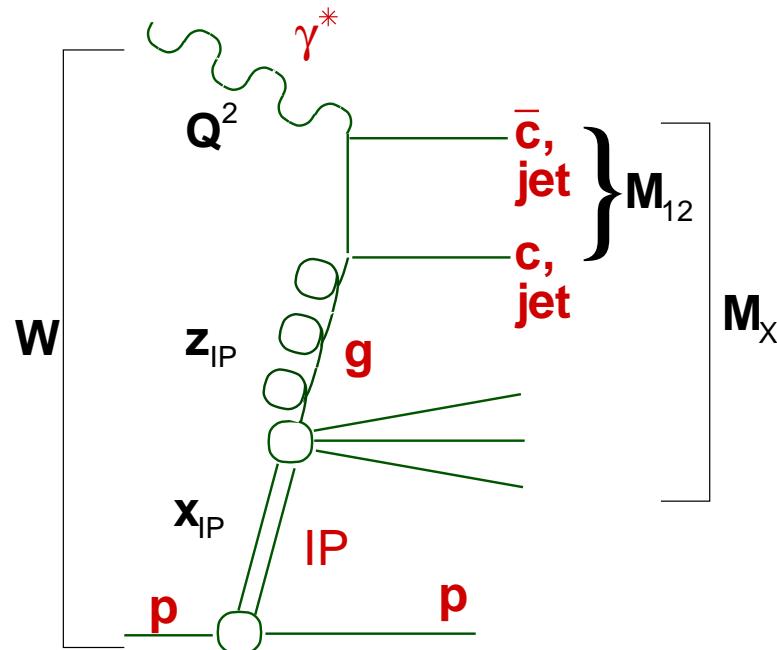
## Extrapolation of QCD fit to high $Q^2$



- New diffractive cross section data for  $200 < Q^2 < 1600 \text{ GeV}^2$
- Well described by evolved pdfs extracted from lower  $Q^2$  data

## Jet and Open Charm Production in Diffractive DIS

Test QCD factorization by applying dpdf's to final state cross sections ...



$Q^2$ : Photon virtuality

$W$ :  $\gamma^* p$  CMS energy

$M_X$ : mass of diffractively produced system

$M_{12} = \sqrt{\hat{s}}$ : mass of two jets /  $c\bar{c}$  pair

$$x_{IP} = \frac{Q^2 + M_X^2}{Q^2 + W^2}$$

momentum fraction of diffractive exchange w.r.t. proton

$$z_{IP} = \frac{Q^2 + M_{12}^2}{Q^2 + M_X^2}$$

momentum fraction of diffractive exchange entering hard process

→ High sensitivity to diffractive gluon distribution!

- high  $p_T$  jet production
- $c \rightarrow D^*$  Meson production

## NLO Calculations for Diffractive Final States

- So far mostly LO Monte Carlo programs with parton showers used
- QCD factorization: Hard scattering cross section same as for normal DIS
- NLO important to describe non-diffractive Jet production

→ use standard NLO programs for jets and heavy quarks in DIS ( $\mathcal{O}(\alpha_s^2)$ )

### Diffractive DIS Jets:

Use DISENT (Seymour)

c.f. Hautmann [JHEP 0210 (2002) 025]

Calculate NLO cross section at fixed  $x_{IP}$  by  
running with reduced  $E_p = x_{IP} E_{p,nom.}$

Use diffractive pdf  $p_{i/IP}(z, \mu^2)$

Mul. w/ flux  $f_{IP}(x_{IP}) = \int dt f_{IP}(x_{IP}, t)$

Data integrated over  $x_{IP}$ :

*“ $x_{IP}$  slicing”*

### Diffractive DIS $D^*$ :

Diffractive version of HVQDIS (Harris,  
Smith) by Alvero, Collins, Whitmore  
[hep-ph/9806340]

$x_{IP}, t$  integration numerically

NLO Calculation in massive scheme

Peterson fragmentation

Both Interfaced to H1 diffractive pdf's

## NLO Comparisons with Diffractive DIS Jets

### Data:

Published H1 data:

[Eur. Phys. J. C**20** (2001) 29]

$4 < Q^2 < 80 \text{ GeV}^2$ ,  $0.1 < y < 0.7$ ,  
 $x_{IP} < 0.05$

Jets: CDF cone,  $p_{T,jet} > 4 \text{ GeV}$

But: NLO unstable if  $p_{T,1} \sim p_{T,2}$   
 $\rightarrow$  Data corrected to  $p_{T,1(2)} > 5(4) \text{ GeV}$

### NLO Calculations with DISENT:

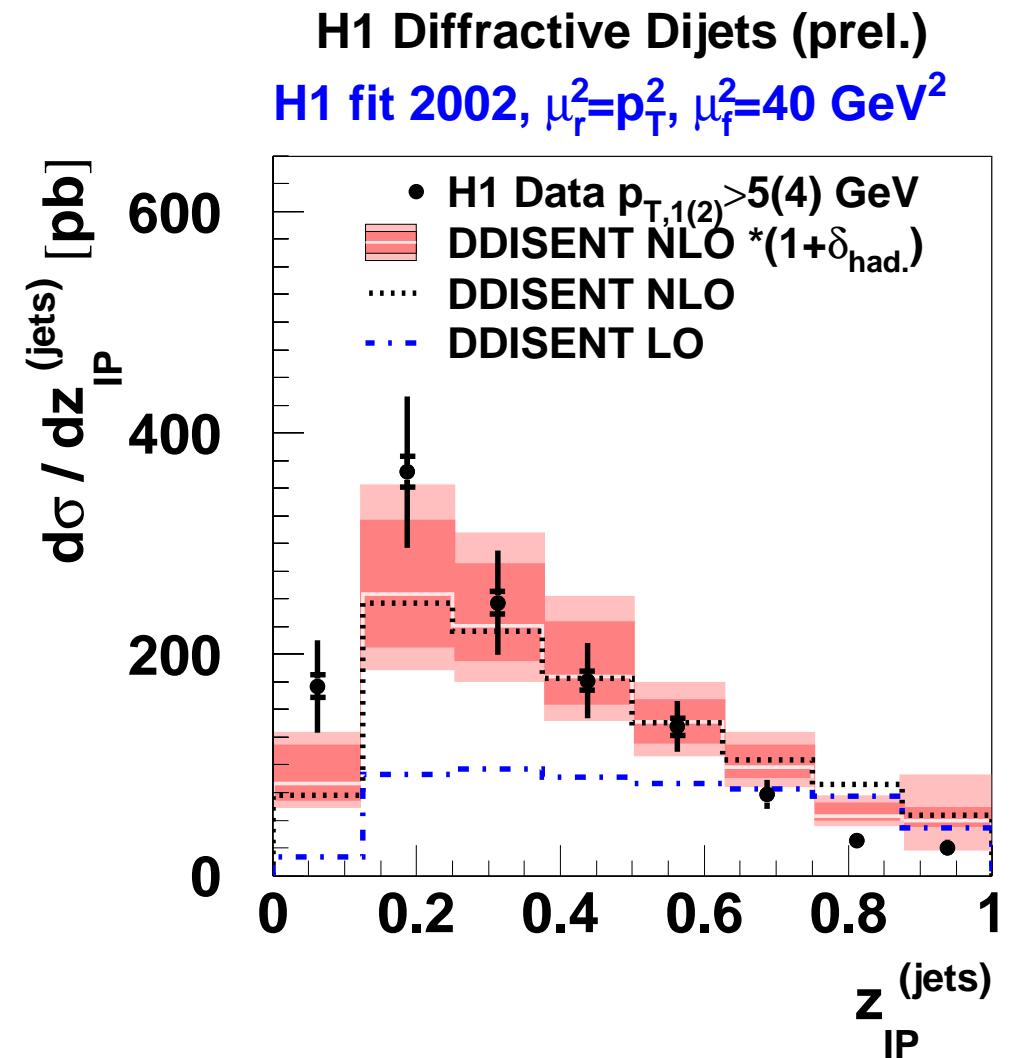
$\mu_r^2 = p_T^2$ ,  $\mu_f^2 = 40 \text{ GeV}^2$

$\Lambda_{QCD}^4 = 0.2 \text{ GeV}$  (as in QCD fit)

Hadronization corrections applied

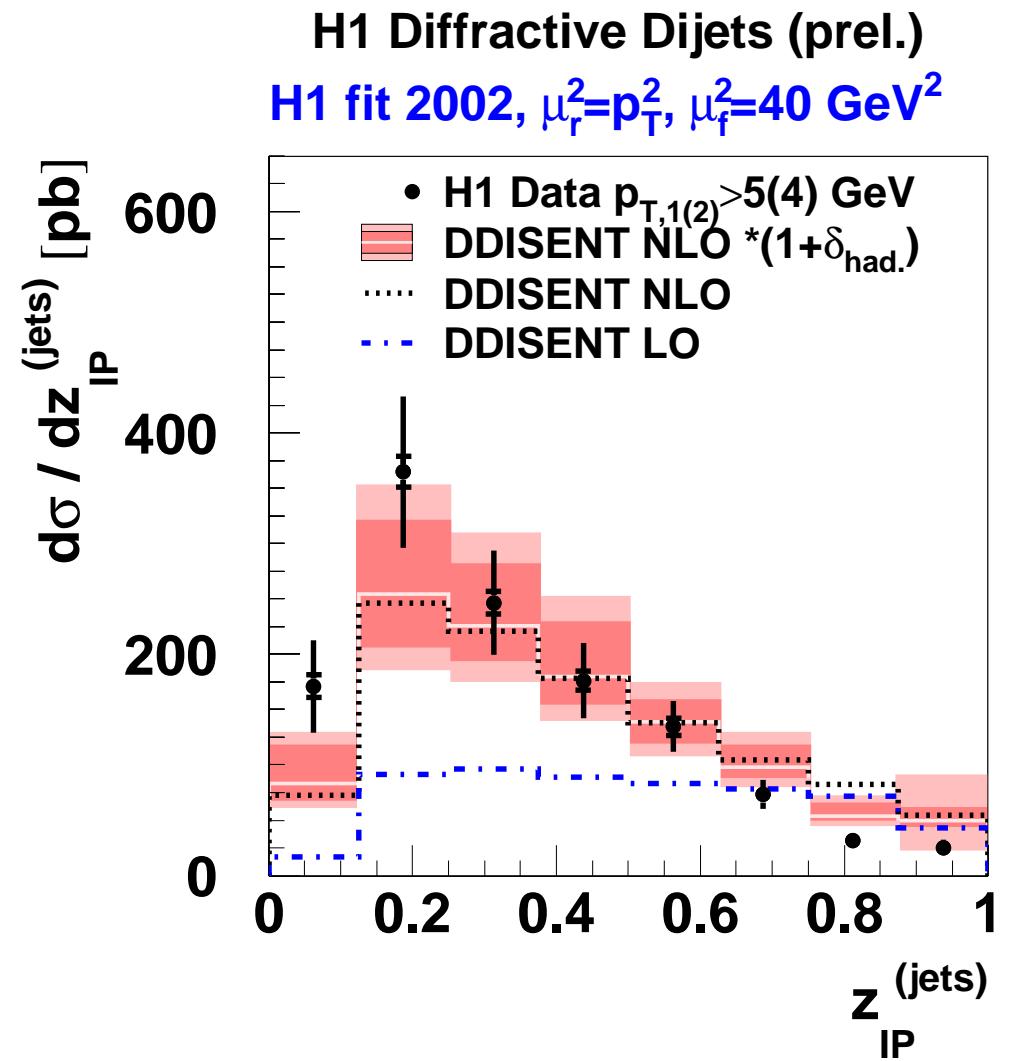
Inner band:  $0.25\mu_r^2 \dots 4\mu_r^2$

Outer band includes unc. in hadr. corr.



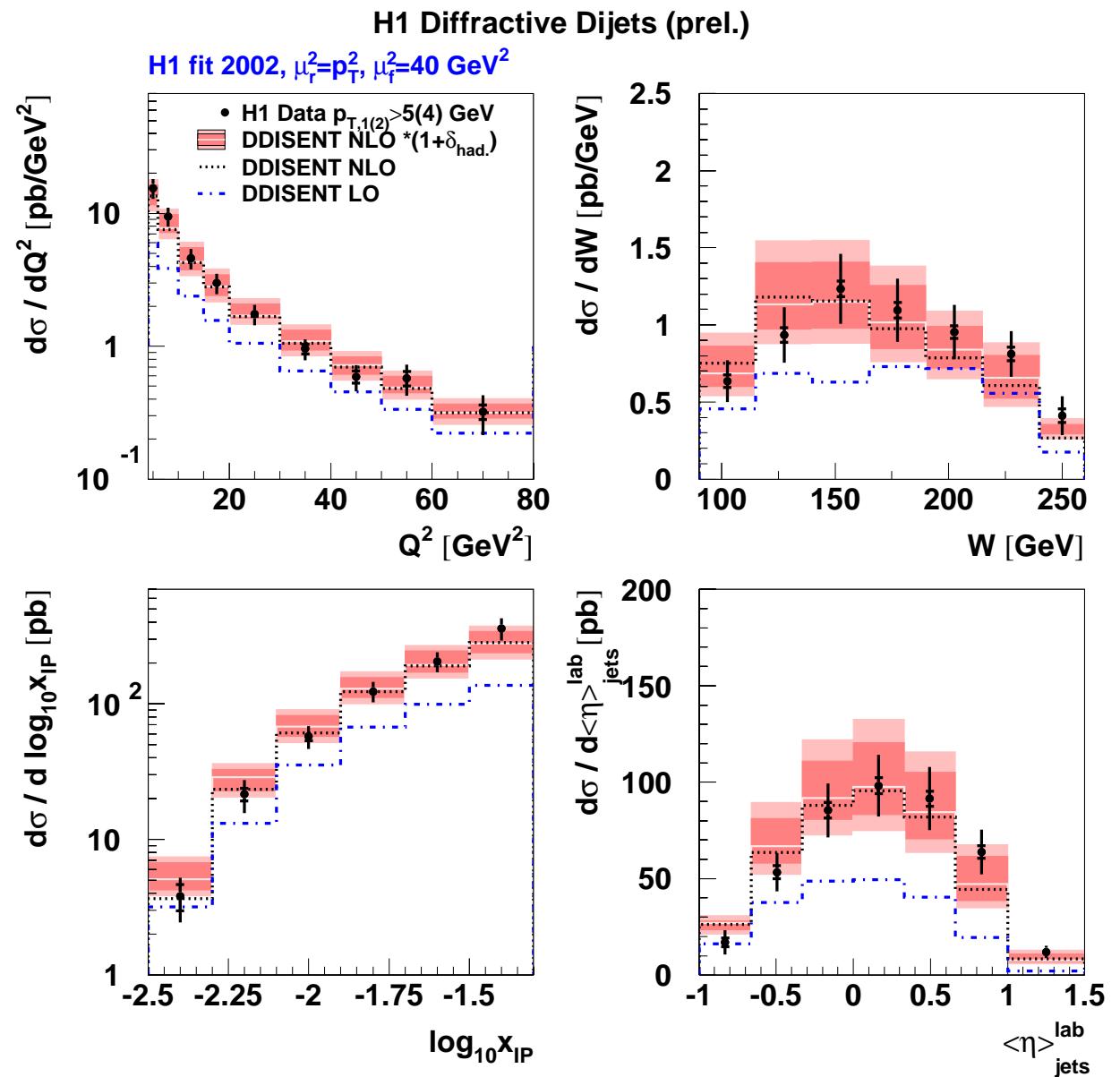
## NLO Comparisons with Diffractive DIS Jets (cont.)

- Cross section differential in  $z_{IP}$
- LO Calculation too low,  
shape of data not reproduced  
(note: w/o parton showers!)
- Size of NLO correction on  
average factor  $\sim 2$  (due to low jet  $p_T$ )
- NLO, corrected for hadronization:  
reasonable description in shape  
and normalization
- Renormalization scale unc.  $\sim 20\%$
- Not shown: pdf uncertainty  
(gluon at high  $z_{IP}$ )



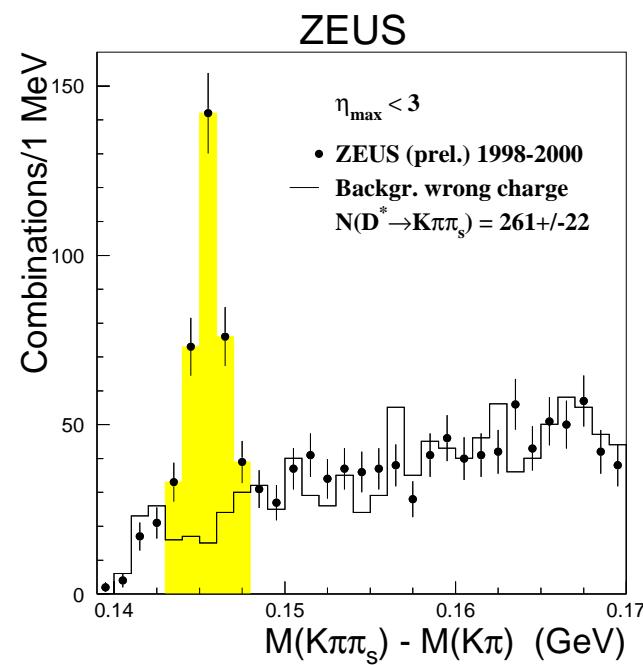
## NLO Comparisons with Diffractive DIS Jets (cont.)

- Further Cross sections:
- Size of NLO Corrections decreasing with  $Q^2$  (and  $p_T$ , not shown)
- Reasonable agreement with NLO calculation



## Diffractive Open Charm in DIS

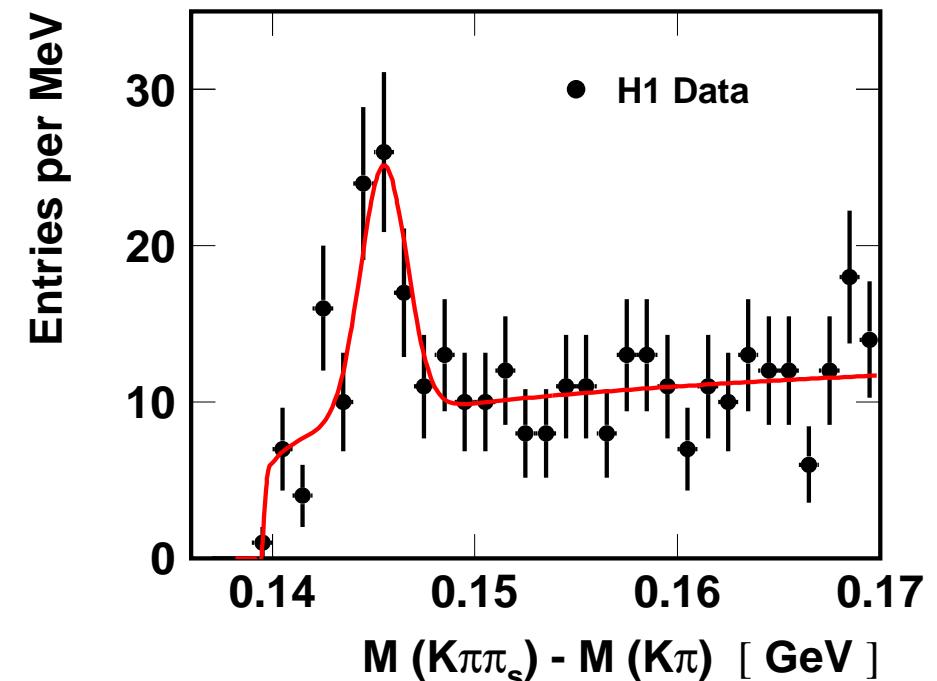
Use  $D^* \rightarrow D_0\pi_s \rightarrow K\pi\pi_s$



$$1.5 < Q^2 < 200 \text{ GeV}^2$$

$$x_{IP} < 0.035$$

$$p_{T,D^*} > 1.5 \text{ GeV}, |\eta_{D^*}| < 1.5$$



$$2 < Q^2 < 100 \text{ GeV}^2$$

$$x_{IP} < 0.04$$

$$p_{T,D^*}^* > 2 \text{ GeV}, |\eta_{D^*}| < 1.5$$

So far measurements statistics limited

## NLO Comparisons with Diffractive DIS $D^*$ (H1)

### NLO Calculations with diffr. HVQDIS:

$$\mu_r^2 = \mu_f^2 = Q^2 + 4m_c^2$$

$$\Lambda_{QCD}^4 = 0.2 \text{ GeV (as in QCD fit)}$$

Peterson Fragmentation:  $\epsilon = 0.078$

$$m_c = 1.5 \text{ GeV}, f(c \rightarrow D^*) = 0.233$$

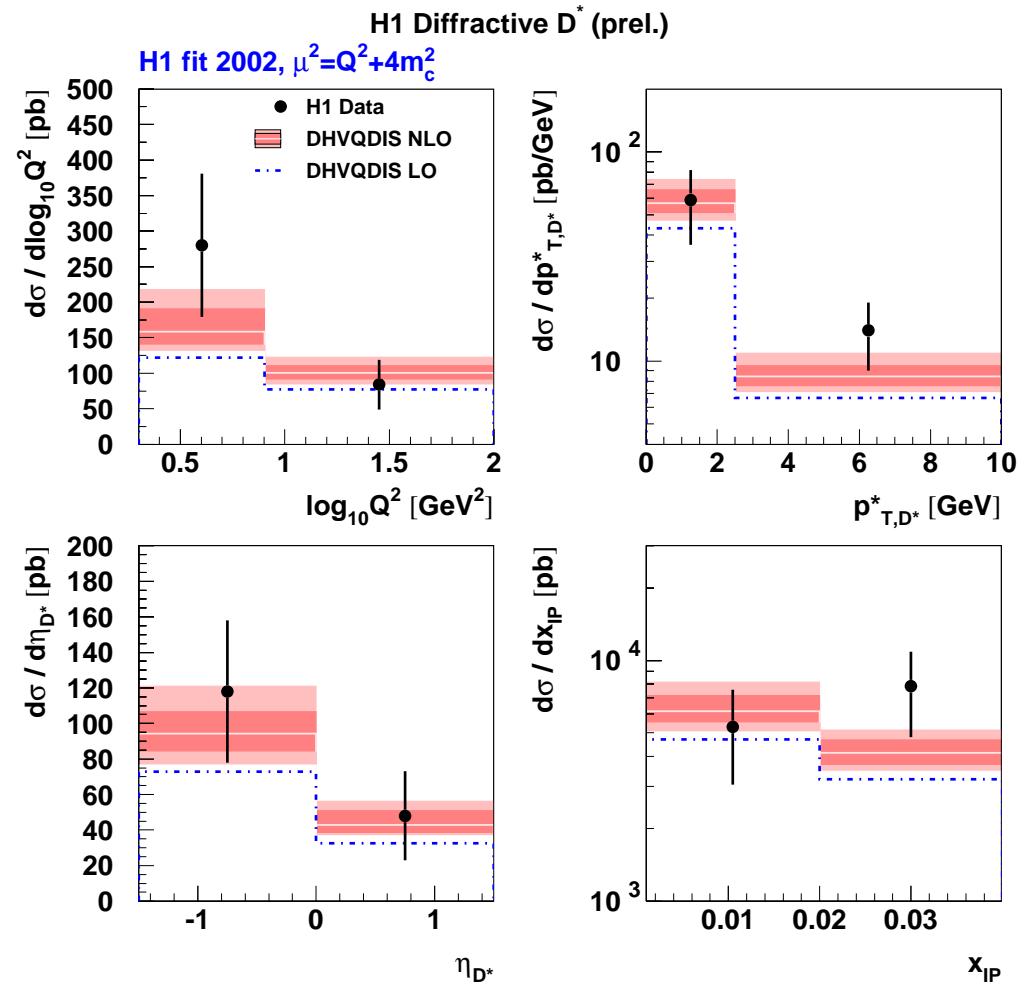
Inner NLO error band:  $0.25\mu_r^2 \dots 4\mu_r^2$

Outer band also includes

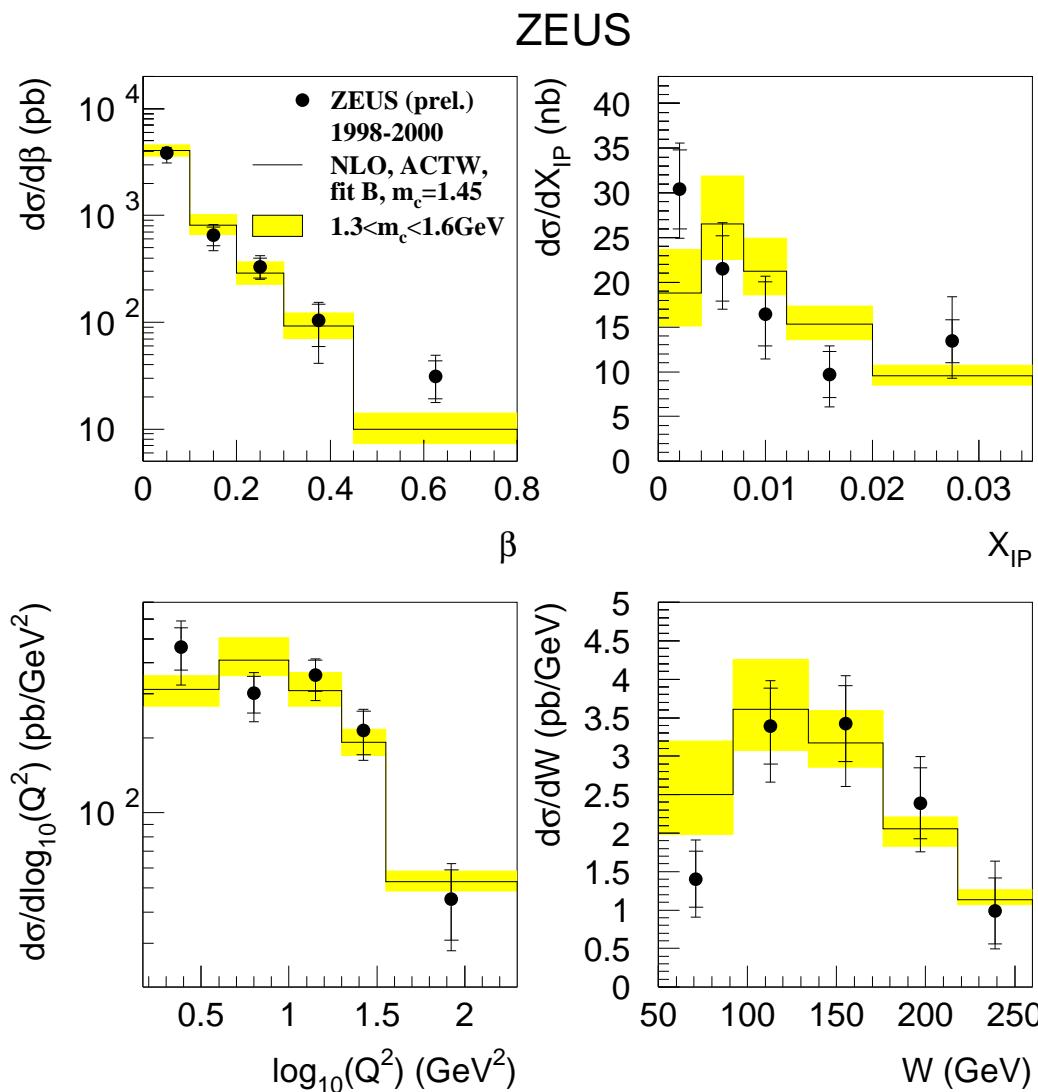
- $1.35 < m_c < 1.65 \text{ GeV } (\pm 12\%)$
- $-0.035 < \epsilon < 0.100 \text{ (+21/ - 7\%)}$

Good agreement in shape and normalization within uncertainties

Size of NLO correction smaller than for dijets



## Diffractive $D^*$ in DIS (ZEUS)

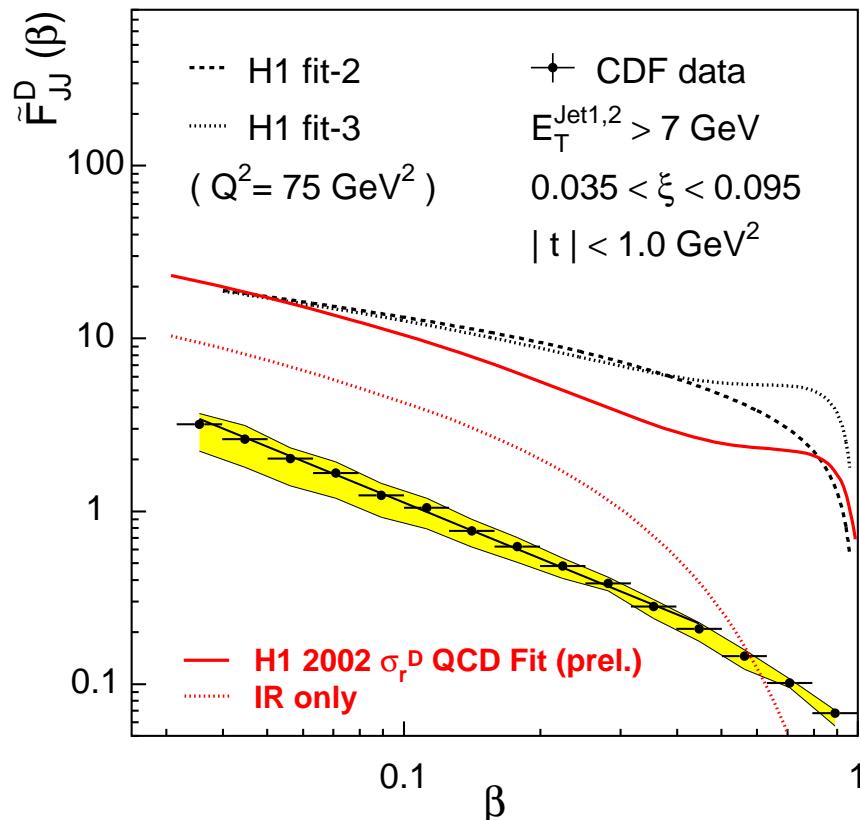


- Theory: gluon dominated pdf's from inclusive fits (ACTW), interfaced to NLO matrix elements
- Differential cross sections well described by calculation!

$\Rightarrow$  Support for QCD factorization in diffractive DIS!

## Diffractive Dijets at the Tevatron (CDF)

Use pdf's to predict hard diffraction in  $pp$ :



- Serious breakdown of factorization observed if HERA pdf's transported to TEVATRON:
- Prediction based on H1 pdf's one order of magnitude above CDF data
- Also observed for other processes:  
Relative rate of diffractive processes  $\sim 1\%$

Due to presence of second hadron in initial state?

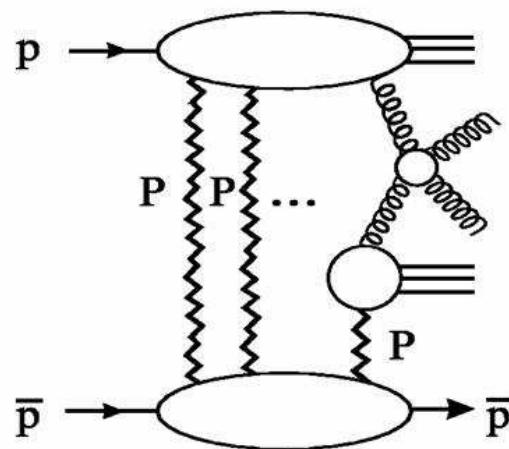
Spectator interactions/rescattering effects break up  $\bar{p}$ , “rapidity gap survival probability”

## Understanding Factorization Breaking at the Tevatron

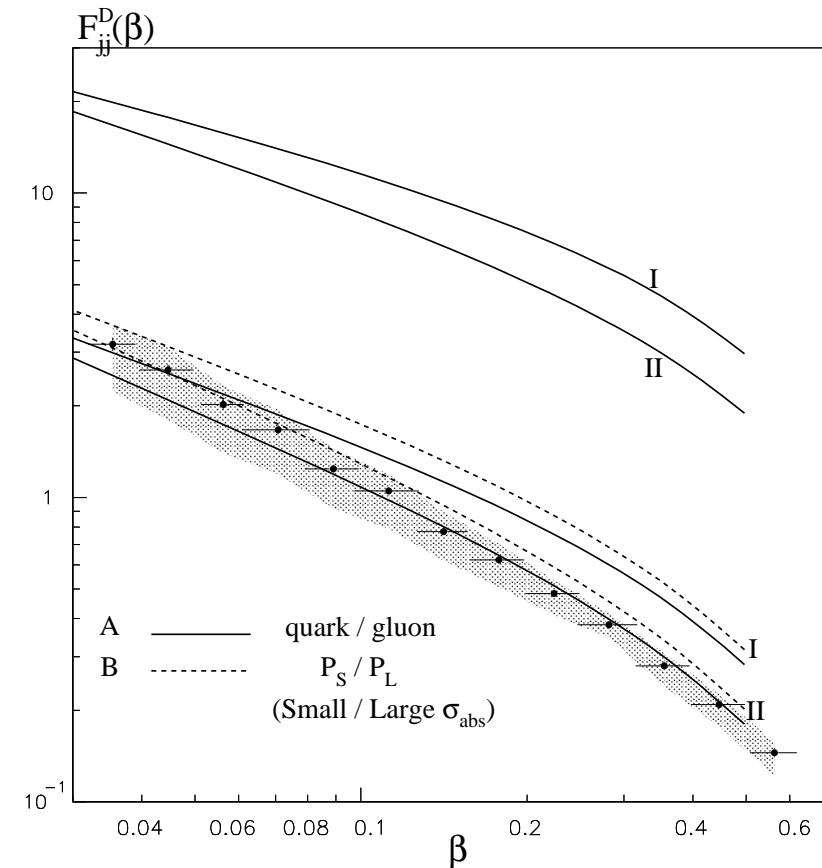
For Example:

Model by Kaidalov, Khoze, Martin, Ryskin  
(KKMR)

Soft rescattering corrections  
of spectator partons



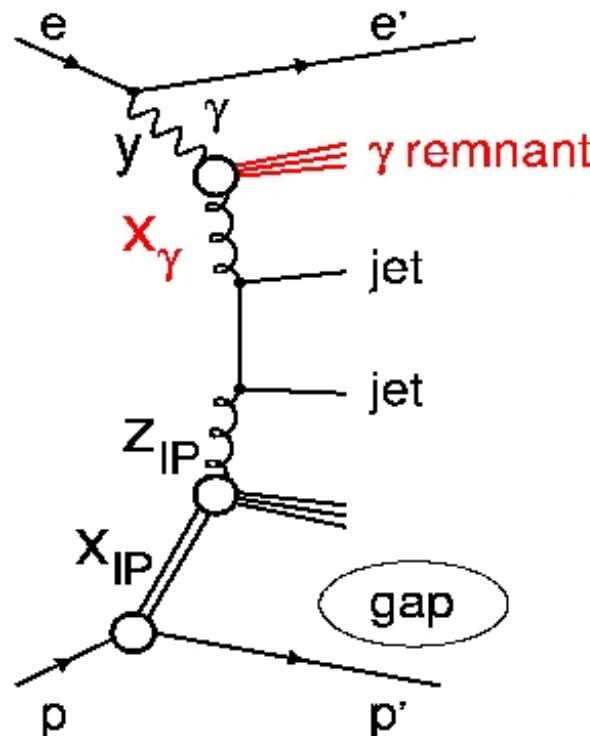
[Two-component eikonal model]



Reasonable description using  
HERA pdf's + rescattering corrections

## Dijets in Diffractive Photoproduction ( $Q^2 \sim 0$ )

Real photon  $\sim$  hadron: Look at HERA in photoproduction ...



Real photon may develop **hadronic structure**  
 $\rightarrow$  similar to hadron-hadron interactions

$x_\gamma$ : Momentum fraction of photon entering  
 the hard process

- $x_\gamma = 1$ : Direct interaction, similar to DIS
- $x_\gamma < 1$ : Resolved interaction, similar to hadron-hadron scattering

- Does QCD factorization also work in diffractive photoproduction (although not proven)?
- Is there a dependence on  $x_\gamma$ ?
- Can factorization breaking w.r.t. Tevatron be understood?

## Dijets in Diffractive Photoproduction

H1 data:

$$Q^2 < 0.01 \text{ GeV}^2, 0.3 < y < 0.65$$

$$x_{IP} < 0.03$$

Jets: incl.  $k_T$  algo.

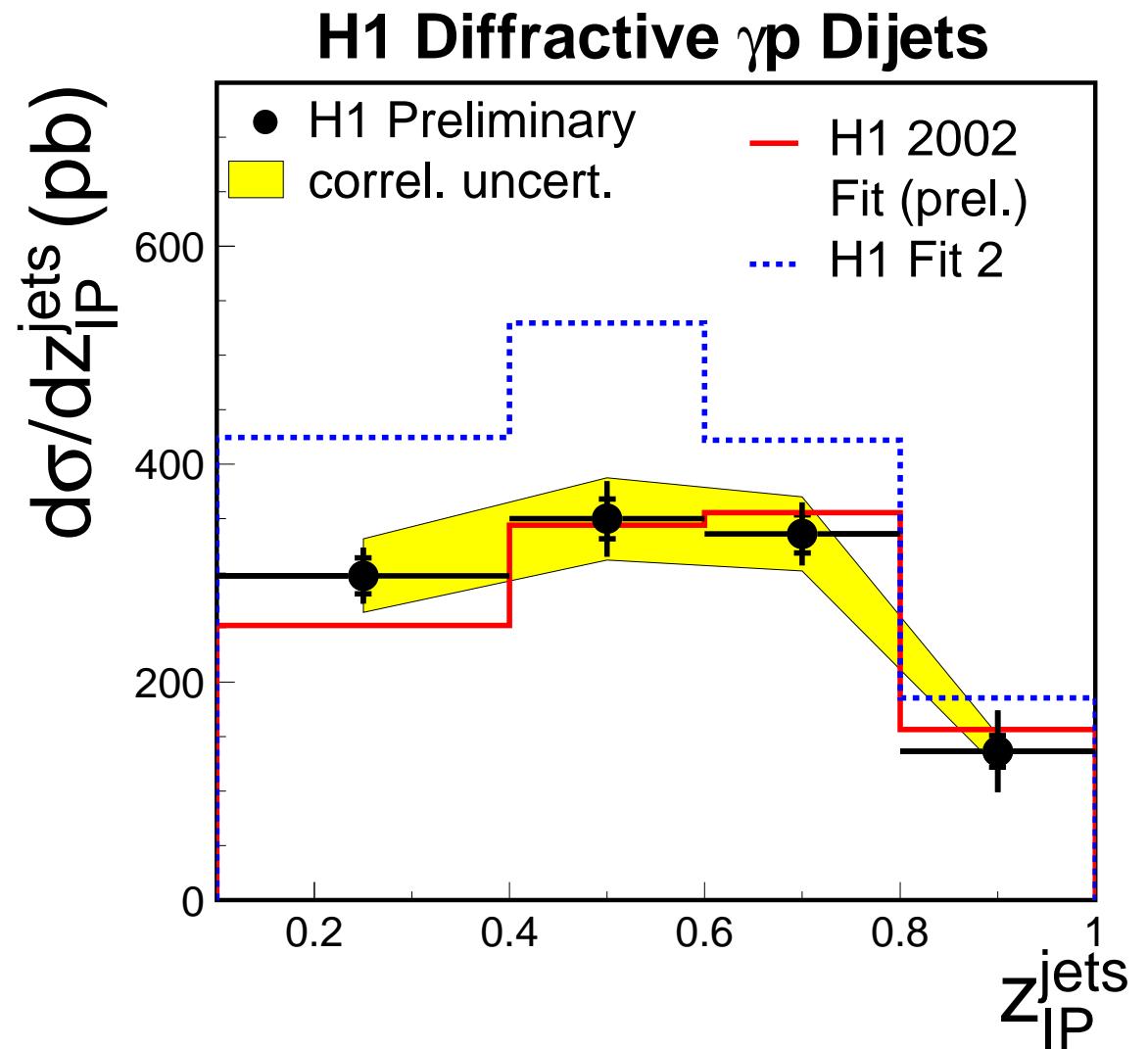
$$p_{T,1(2)} > 5(4) \text{ GeV}$$

Monte Carlo comparisons:

LO ME + parton showers: RAPGAP

$$\mu_r^2 = p_T^2$$

- New 2002 LO fit describes data very well
- Old “H1 fit 2” too high, but large uncertainties



## Dijets in Diffractive Photoproduction

- Cross section as a function of  $x_\gamma$
- New 2002 fit describes direct and resolved contribution

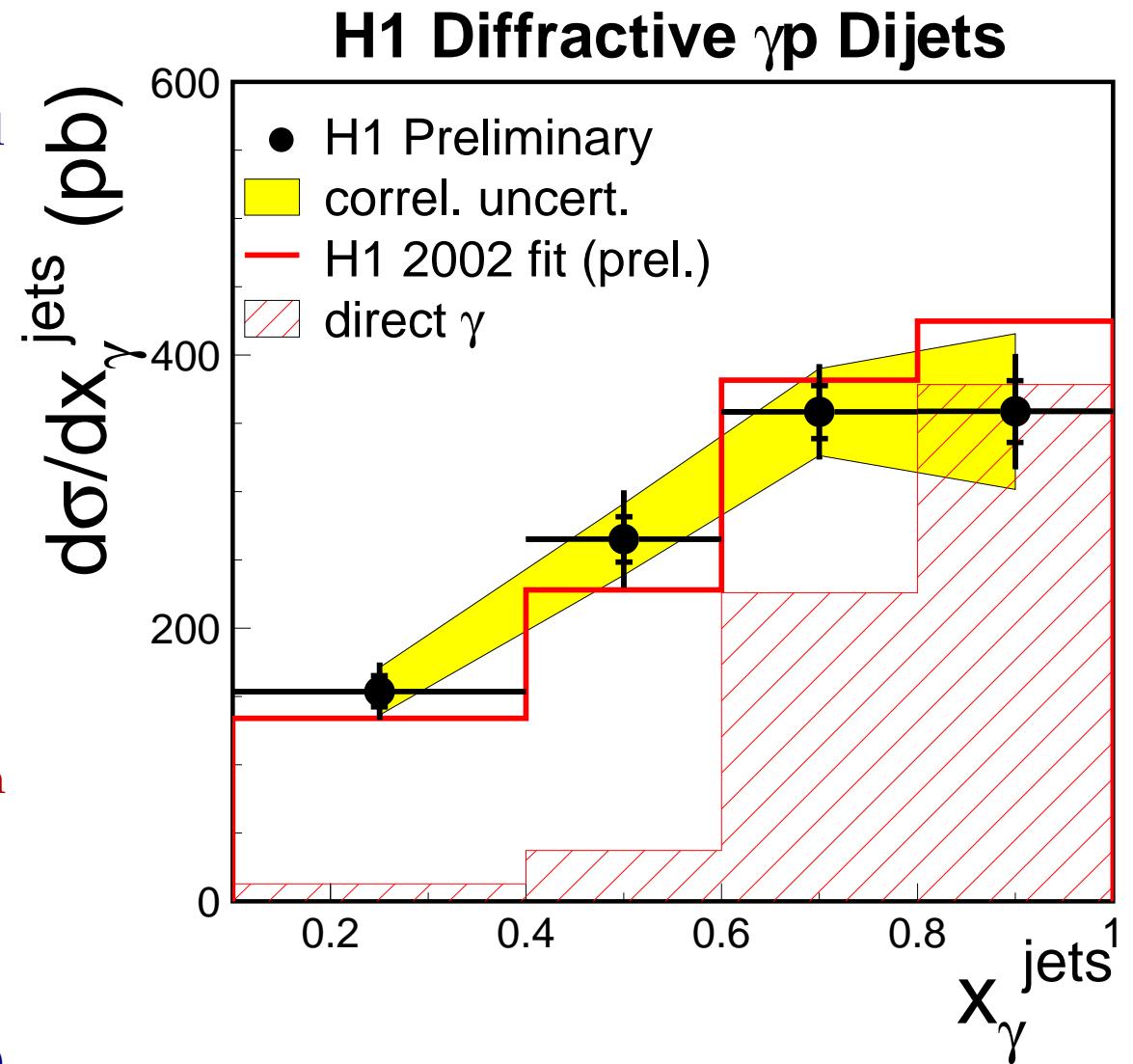
Direct comparison DIS vs  $\gamma p$ :

$$\frac{\left(\frac{Model}{Data}\right)_{\gamma p}}{\left(\frac{Model}{Data}\right)_{DIS}} = 1.25 \pm 0.30 (\text{exp.})$$

Within uncertainties **no suppression** of  $\gamma p$  w.r.t. DIS diffractive jets

Independent of fit

(NLO Calculations being worked on...)



## Conclusions

**HERA-I has told us:**

- Diffractive DIS at HERA: Investigate **quark/gluon structure of diffraction**
- High precision HERA data in large kinematic range available
- Diffractive pdf's of proton have been determined at NLO
- Comparison with jets/charm: **Self-consistent QCD picture of diffractive DIS to NLO**
- Does factorization also hold in diffractive photoproduction? (Need NLO calc.)

**From HERA to the LHC (via TEVATRON):**

- HERA-II to provide a lot **more data**  
(in particular using the H1 VFPS)
- Understanding of **factorization breaking mechanism**  $ep$  vs  $pp$  needed
- Need diffr. pdf's in **kinematic range relevant for LHC!**
- Can **diffractive pdf's + non-factorizing mechanism be combined** in a sensible way to obtain predictions for the LHC (e.g. diffractive Higgs)?